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Compiler design

Lexical Analysis [Regular Expression
Finite Automata]
parsing [CFM DPDA]
Semantic Analysis [Context Sensitive
Grammar]
Intermediate code generation [Attribute grammar]
code optimization
code generation and Runtime Environment

Grammar

DEF:- Set of rule used to describe string
of language.

$G = (V, T, P, S)$

$V \Rightarrow$ Set of variable (non-terminals)

$T \Rightarrow$ Set of terminal

$P \Rightarrow$ No. of production

$S \Rightarrow$ Starting symbol

For every language there exists a grammar
and every grammar represents rules of
some language.

$$\alpha = \{a^n b^n \mid n \geq 1\}$$

$$\{ab, aabb, \text{aaaabbbb} \dots\}$$

Recursion

then grammar for this:

$$S \rightarrow ab \mid \underline{a} S b$$

recursion representation

$$\alpha = \{a^n b^m c^m \mid n, m \geq 1\}$$

$$\{abc, aabbcc, \text{aaaabbbbcccc} \dots\}$$

$$S \rightarrow \underline{A} B$$

$$A \rightarrow \underline{a} b \mid \underline{a} A b$$

$$B \rightarrow \underline{c} \mid \underline{c} B$$

production

$$V = \{S, A, B\} \quad p.$$

$$T = \{a, b, c\}$$

$$\# \quad \alpha = \{a^n \underline{b^m} \underline{c^m} d^n \mid m, n \geq 1\}$$

$$S \rightarrow a A \underline{d} \mid a s d$$

$$A \rightarrow b c \mid b A c \quad \{b^m c^m\}$$

Find the grammar that represent all, palindromes of english language.

$$S \rightarrow \underbrace{aSa | bSb | cSc}_{26} | \dots | \underbrace{zSz}_{26} | \underbrace{a|b|c}_{26} | \underbrace{aa|bb|cc}_{26}$$

= 78.

Identify ^{language} ~~grammar~~ generated by this grammar:

$$S \rightarrow aS | bS | a | b$$

Derivation: process of generating strings from the given grammar by replacing left hand side grammar by its corresponding right side part.

$$\alpha = \{a, b, aa, bb, ab, ba\}$$

$$= (a+b)^+ A$$

$a^n b^m c^k \geq 1$ it can't be generated

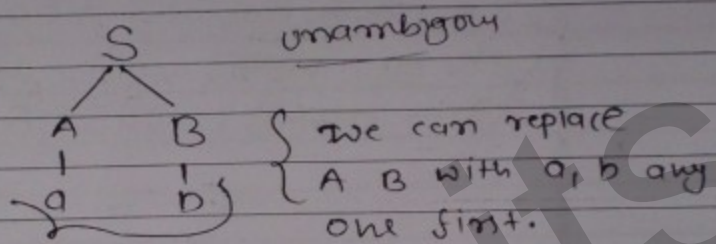
$$S \rightarrow aSBC \quad \text{by type 2 grammar}$$

$$S \rightarrow abc$$

$$cB \rightarrow Bc$$

$$bB \rightarrow bb$$

Q1

 $S \rightarrow AB$ $A \rightarrow a$ $B \rightarrow b$ 

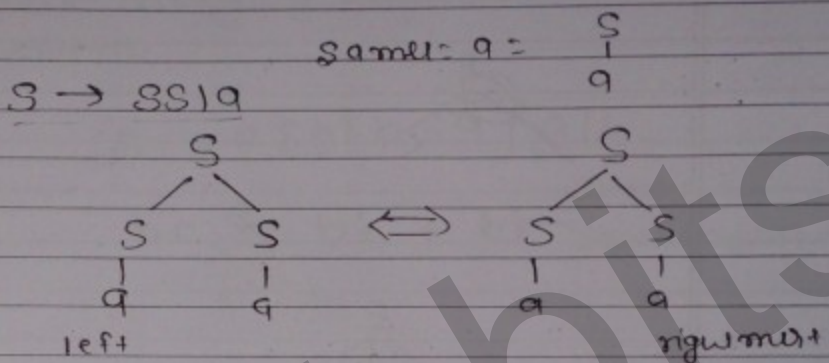
if we replace A by a first then it is called left most derivation else it is right most derivation.

#1 E.M.D:- Left most non terminal replace, by it corresponding right hand side part. In the derivation process. At every step is known as L.M.D.

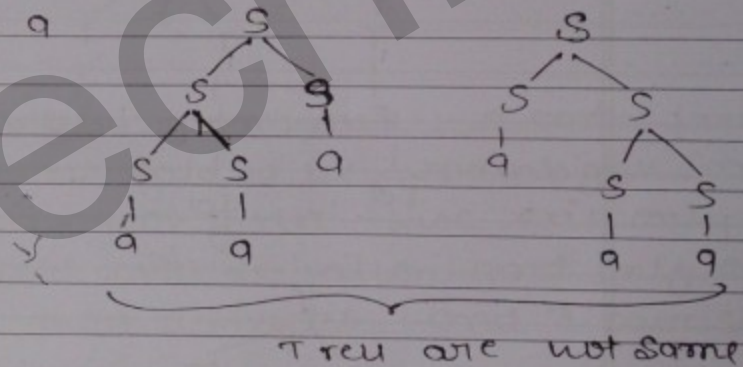
#1 Right Most non terminal replace by its corresponding right hand side part at every step in derivation process is R.M.D.

The derivation may be left most for right most derivation or random derivation.

but in parsing we will use left most derivation or right most derivation.



\Rightarrow ~~SSa~~
 \Rightarrow aaa

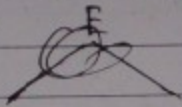
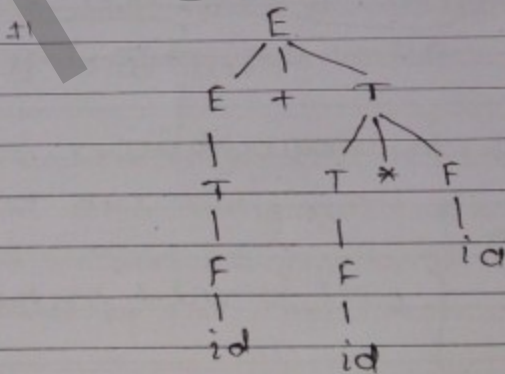
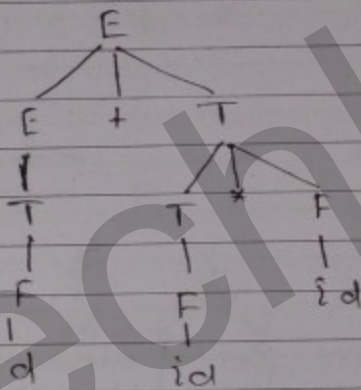


so it is unambiguous.

$\left. \begin{array}{l} S \rightarrow aSb \\ S \rightarrow ab \\ S \rightarrow SS \end{array} \right\}$ well formed prefixes.

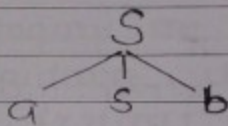
Q1

~~$E \rightarrow E + T$~~ $E \rightarrow E + T / T$
 $T \rightarrow T * F / F$
 $F \rightarrow id$


 $id + id * id$


- #1 Note :- To check the ambiguity in context free grammar there is no algorithm since ambiguity problem is "undecidable" problem.

$$S \rightarrow aSb \mid bSa \mid a \mid b$$



Small

Small string = a

- #1 unambiguous grammar :- A context free grammar said to be unambiguous for "all string of given" there exist only one left most derivation and only one right most derivation and it parse string.

For one string one left most derivation and one right most derivation exist. both have to produce only one parse tree.

$S \rightarrow aSb \mid ab$ grammar is
 a unambiguous are not.

Au \Rightarrow undecidable.

NOTE :- It is ~~im~~ impossible to
 eliminate, ambiguity from,
 every ambiguous context free grammar
 because, there is no generalized algorithm
 hence, elimination of ambiguity problem
 is also undecidable problem.

A ambiguous grammar for which, elimination
 of ambiguity is not possible, it called,
 as inherently ambiguous grammar.

$$\alpha = \{a^i b^j c^k \mid i=j \text{ @ } j=k\}$$

$$\alpha = \{a^n b^n c^m \mid n,m \geq 1\} \cup \{a^n b^m c^m \mid n,m \geq 1\}$$

Fortunately No programming language are
 inherently ambiguous.

$$S \rightarrow S_1 | S_2$$

$$S_1 \rightarrow AB$$

$$A \rightarrow aAb | ab$$

$$B \rightarrow cB | c$$

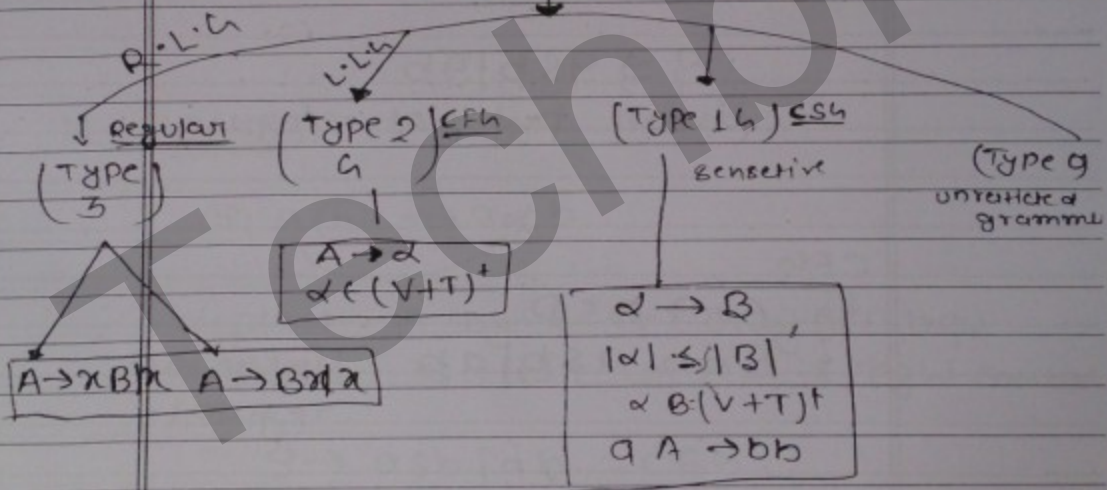
$$S_2 \rightarrow CD$$

$$C \rightarrow cC | a$$

$$D \rightarrow bDc | bc$$

#

Types of grammar



Linear grammar:- In any grammar,

left hand side only one nonterminal
right hand side at most one nonterminal
is present, that is linear grammar.

#1 Linear grammar may be left linear or right linear or middle linear.

#1 If the linear grammar is either left linear or right linear then it is regular.

#1 All regular grammar are linear grammar but all linear grammar need not be linear.

$S \rightarrow aSb | ab$
linear but not regular.

CFN

eg $A \rightarrow BCD$

$S \rightarrow aSb | ab$ = linear not regular.

CSL

$aA \rightarrow bb$

left context

$S \rightarrow AB$

$aA \rightarrow ab$

$B \rightarrow a$

CSL

Regular grammar:

$$S \rightarrow aS \mid bS \mid a$$

$$\begin{array}{l} \text{H} \quad S \rightarrow LA \\ \quad \quad A \rightarrow LA \mid dA \mid \epsilon \end{array} \quad \left. \vphantom{\begin{array}{l} S \\ A \end{array}} \right\} \text{RLL}$$

$$S \rightarrow CS \mid SS \mid \epsilon = \text{CFLL}$$

H CSL

$$\textcircled{a} A \textcircled{b} \rightarrow a \alpha b$$

replace A by α if only, it has a and b as left context & right context.

$$S \rightarrow aSb \mid ab = \text{CFLL}$$

becoz it is regular we can have either

$$A \rightarrow \alpha B;$$

$$\text{or } A \rightarrow B\alpha;$$

#

- 1) Regular grammars, not have, enough power, to represent syntax of programming language. (Structure) hence to represent syntactic structure of programming language the suitable grammar are context free grammar.
- 2) context free grammar, doesn't have enough power to represent semantic (meaning) of programming language hence to represent semantic of programming language suitable grammar are context sensitive grammar that language context sensitive language.
Hence C language, C++ Java etc language called as context sensitive language.

#

$$S \rightarrow a S b \mid a A b \quad \Rightarrow a S b^2$$

$$A \rightarrow b A \mid b \quad \Rightarrow a b b$$

b, bb--
a bb

$$a^n b^n \quad n < m$$

#1 check if the string is member of grammar or not. It called a parsing.

$$S \rightarrow AB|BC$$

$$A \rightarrow BA|a$$

$$B \rightarrow CC|b$$

$$C \rightarrow AB|a$$

b

a

Ans

First calculation first (First set)

=> 1) The first of a non terminal, gives information regarding that non terminal right hand side available first terminal information.

$$A \rightarrow a \alpha$$

↳ a is a.

$$\text{First}(A) = \{a\}$$

2)

$$A \rightarrow B \alpha$$

$$\text{First of } (A) = \text{First of } (B)$$

$$A \rightarrow B \alpha$$

$$B \rightarrow e$$

$$\text{First}(A) = \{\text{First}(B) - e\} \cup \{\text{first } \alpha\}$$

#1 $S \rightarrow aAB$
 $A \rightarrow b$
 $B \rightarrow c$

calculate first of every, non terminal of this grammar.

S	{a}
A	{b}
B	{c}

#1 $S \rightarrow AB$
 $A \rightarrow a|E$
 $B \rightarrow b$
 $S \rightarrow A$
 $A \rightarrow a$

S	{a, b}
A	{a, E}
B	b

#1 $S \rightarrow AB$
 $A \rightarrow a$
 $B \rightarrow b|E$

S	{a}
A	{a}
B	{b, E}

$$\begin{aligned} \#1 \quad & E \rightarrow TE' \\ & E' \rightarrow +TE' \mid \epsilon \\ & T \rightarrow FT' \\ & T' \rightarrow *FT' \mid \epsilon \\ & F \rightarrow id \end{aligned}$$

$$\begin{aligned} E &= \{id\} \\ E' &= \{+, \epsilon\} \\ T &= \{id\} \\ T' &= \{*, \epsilon\} \\ F &= \{id\} \end{aligned}$$

$$\#1 \quad S \rightarrow A^e A^e B \mid B^e B^e A$$

$$A \rightarrow e$$

$$B \rightarrow c$$

$$S = \{e, a, b\}$$

$$A = \{e\}$$

$$B = \{c\}$$

$$\left(\begin{array}{l} S \rightarrow A = \{e\} = \{a\} \\ S \rightarrow B = \{c\} = \{b\} \\ S \rightarrow \{a, b\} \end{array} \right)$$

$$\#1 \quad S \rightarrow A^e C B \mid C^e B \mid B^e A \{$$

$$A \rightarrow d a \mid B C \quad \{d\} \quad \{d, a, h, b, a, \epsilon\}$$

$$B \rightarrow g \mid \epsilon = \{g, \epsilon\} \quad \{d, a, h, \epsilon\}$$

$$C \rightarrow h \mid \epsilon = \{h, \epsilon\} \quad \{$$

$$S = \{d, g\}$$

Q1

$$A \rightarrow A_1 A_2 A_3$$

First of (A_1) contain 5 elements.

First of (A_2) contain 4 elements.

First of (A_3) contain 3 elements.

All first set contain (ϵ) and all element are different. So how many element contain

$$A_1 \rightarrow 5 \quad (1 \text{ '}\epsilon\text{' then take 4)}$$

$$A_2 \rightarrow 4 \quad (3)$$

$$A_3 \rightarrow 3 \quad (2)$$

and last of $A_3 \rightarrow \epsilon$ include ϵ

$$= 4 + 3 + 2 + 1$$

$$= 10.$$

1) Follow (Starting symbol) = $\{\$ \}$

2) $A \rightarrow \alpha B \beta$

$$\text{Follow}(B) = \text{First}(\beta)$$

3) $A \rightarrow \alpha B$

$$\text{Follow}(B) = \text{Follow}(A)$$

$A \rightarrow \alpha B \beta$

$B \rightarrow \epsilon$

[NOTE:- Follow set doesn't include ϵ]

$$\text{Follow}(B) = \{ \text{First}(\beta) - \epsilon \} \cup \text{Follow}(A)$$

$E \rightarrow TE'$

$E' \rightarrow +TE' | \epsilon$

$T \rightarrow FT'$

$T' \rightarrow *FT' | \epsilon$ $\{ *, \epsilon \}$

$F \rightarrow id$

~~$E = \{ \epsilon \}$~~ Follow = $\{ \$ \}$

Follow = $E' = \{ \$ \}$

Follow(T) = $\{ +, \$ \}$

$T \rightarrow E' \rightarrow \epsilon$ generate ϵ

then take first of E'

$\{ +, \epsilon \}$

↓ exclude $\Rightarrow \{ +, \$ \}$

Follow(T') = $\{ +, \$ \}$

Follow(F) = $\{ *, +, \$ \}$

#1

$$S \rightarrow \textcircled{A} \textcircled{a} \textcircled{A} \textcircled{b} \mid \textcircled{B} \textcircled{b} \textcircled{B} \textcircled{a}$$

$$A \rightarrow \epsilon$$

$$B \rightarrow \epsilon$$

$$S = \{ \$ \}$$

$$A = \{ a, b \}$$

$$B = \{ b, a \}$$

#1

$$S \rightarrow \textcircled{A} \textcircled{d} \textcircled{B} \mid \textcircled{d} \textcircled{b} \mid \textcircled{B} \textcircled{a}$$

$$A \rightarrow d \mid \textcircled{B} \textcircled{c}$$

$$B \rightarrow g \mid \epsilon = \{ g, \epsilon \}$$

$$C \rightarrow h \mid \epsilon = \{ h, \epsilon \}$$

$$S = \{ \$ \}$$

$$A = \{ h, g, \$ \}$$

$$B = \{ \$, a, h, g \}$$

$$C = \{ g, \$ \} \cup \{ g, \$, b, h \}$$

$$\#1 \quad S \rightarrow a \textcircled{A} b B \mid b \textcircled{A} a \textcircled{B} \mid \epsilon$$

$$\rightarrow A \rightarrow S$$

$$B \rightarrow S$$

$$\text{First}(S) = \{a, b, \epsilon\}$$

$$\text{First}(A) = \{a, b, \epsilon\}$$

$$\text{First}(B) = \{a, b, \epsilon\}$$

$$\text{Follow}(S) = \{\$, a, b\}$$

$$\text{Follow}(A) = \{b, \epsilon\}$$

$$\text{Follow}(B) = \{a, \epsilon\}$$

#1 What is the regular expression that represent all the substring of string - delhi.

Substring of delhi	TOC
5 - d, e, l, h, i ✓	T, O, C - 3
4 - de, el, lh, hi ✓	TO OC - 2
3 - del, elh, lhi ✓	TOC - 1
2 - delh, elhi ✓	
1 - delhi ✓	
Total	$\left[\frac{n(n+1)}{2} + 1 \right]$

Q1

What is regular expression that generates letter and digit. And every string is starting with letter and length of string is at most "32".

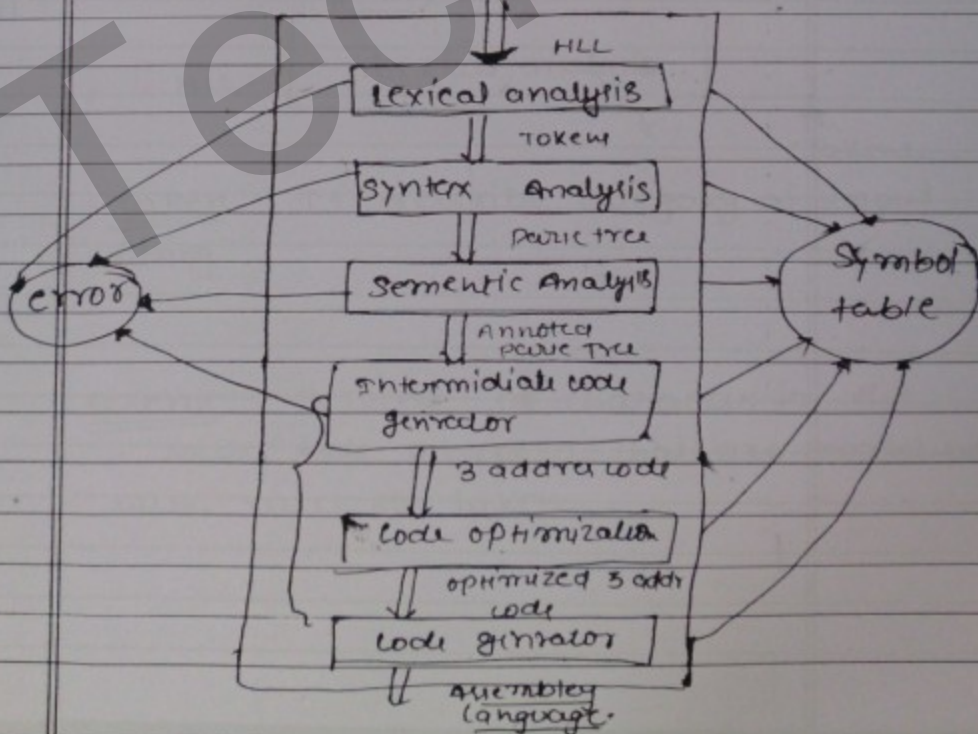
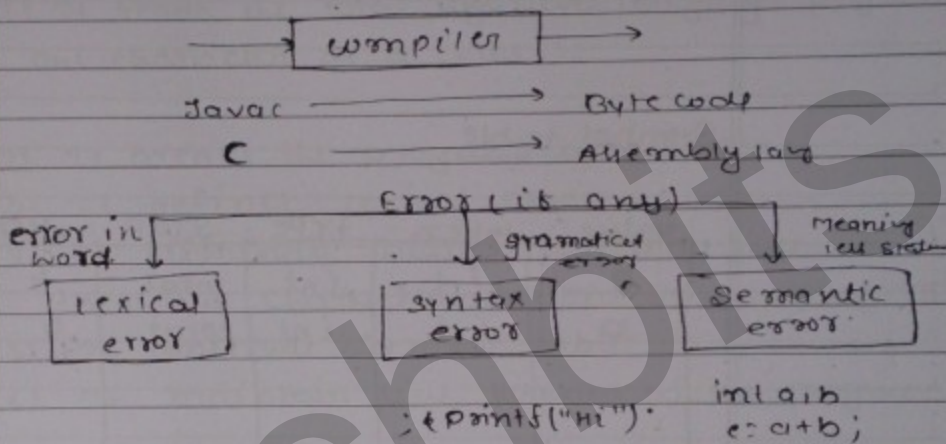
Ans

$\Sigma = \{a, b\}$ of length 5

$(a + b + \epsilon)^5$

A) $l \cdot (l + d + \epsilon)^{31}$

compiler :- is a program that translate a program written in one language into an equivalent program in another language.



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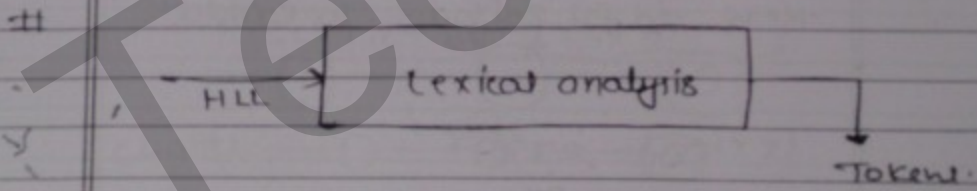
Symbol table is a data structure that contains information regarding variable and constant of the program along with its attribute values.

Symbol table

value	token	type	Scop	Memory
a	id	int	local	4
b	id	int	local	4

lexical analysisfunctionalities

- 1) It reads the total high-level language programs one character at a time.
- 2) It breaks the program into tokens.
- 3) It defines lexical error.
- 4) It eliminates blank, comment lines, new line characters present in the program.
- 5) It constructs symbol table.
- 6) It maintains line number of the program.



Token:- It describes category of input string.

Lexeme:- Sequence of characters in the source ~~code~~ program, that are matched with, rules of token.

int a, b;
↓
Token (keyword)

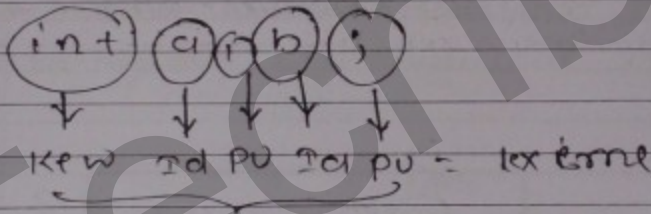
Keyword :- is, else,
for, while.

Identifier :- x1y,
1x

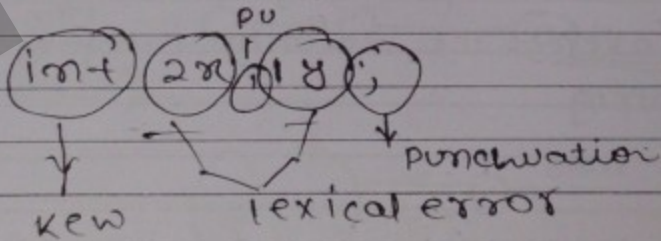
Constant 20, 50.6

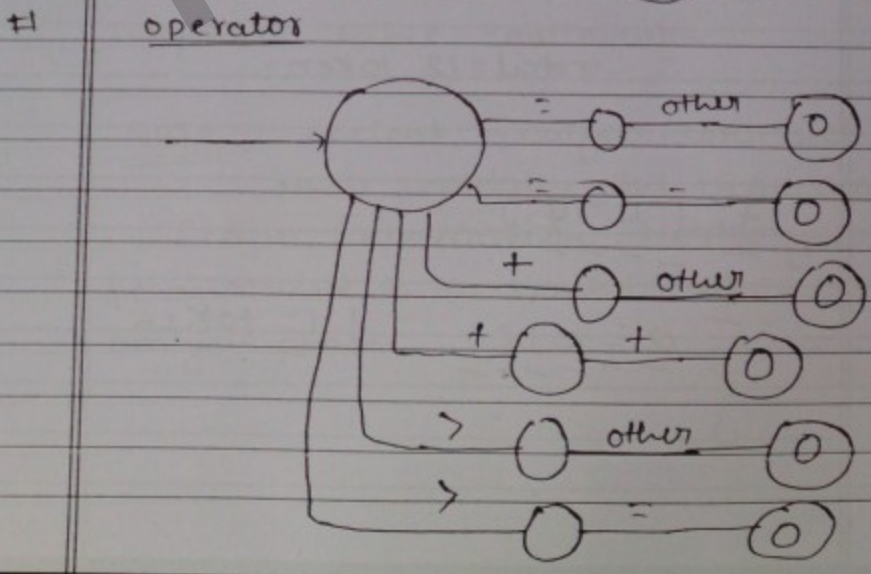
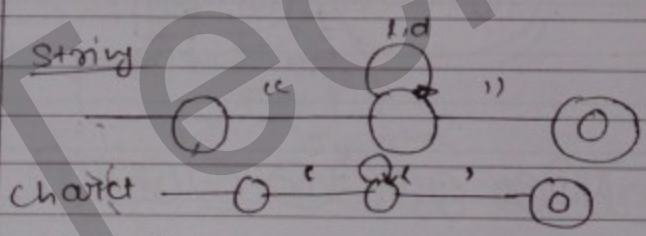
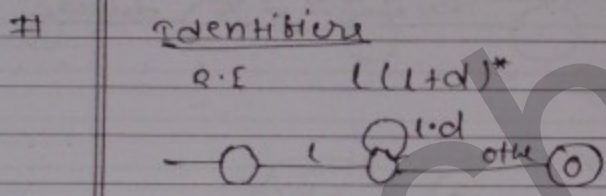
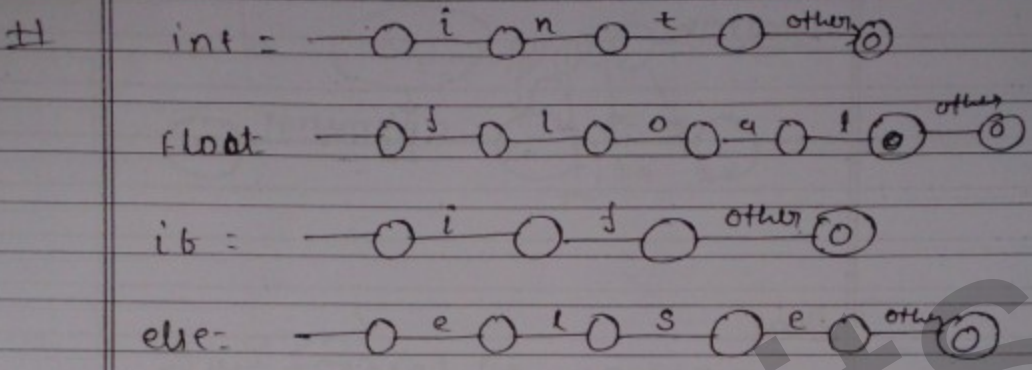
operator :- +, -, *, /, %

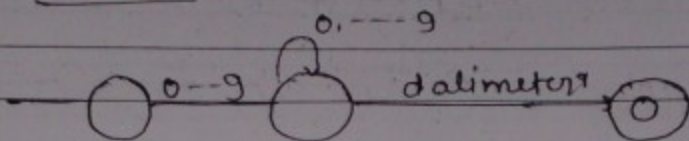
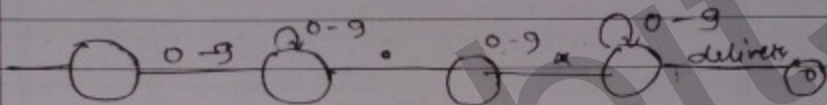
punctuation :-
{, }, (,), \$, %



lexical error





constantReal
 $(0+1+2+...+9)^+ (0+1+2+...+9)^1$


```
int (ny3123) (x9bc);
```

↓ other
↓ other

```
for (i=0; i<=10; i++)
```

= Total = 13 token.

#1

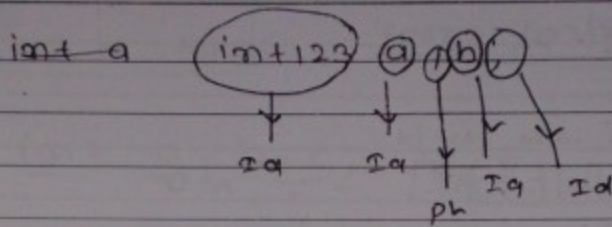
```
f. ( a > b )
```

```
{
```

```
  a = b + c;
```

```
}
```

14 = token

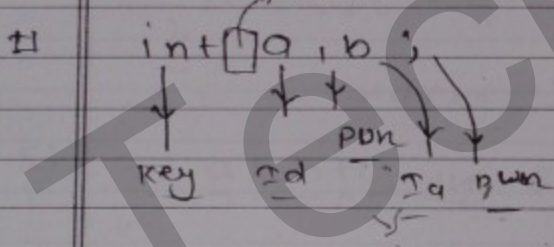


$\frac{1}{10} \frac{1}{2} \frac{1}{3} \frac{1}{4} \frac{1}{5} \frac{1}{6}$

$q = b + c; /* \text{additi.} */$

} = 14 ~~tokens~~ tokens

white space automata also implemented



Symbol table construction.

NOTE :- Lexical analyzer, construct Symbol table, partially. The type information, Scope information, Memory size will be allocated to the symbol table, into semantic analysis phase.

lexical error

PU id op id op id

✓ 1) `[] [a] [=] [b] [a] [c]` = NO

✓ 2) `[c] = [a] + "Hello";` NO
id op id op string

✓ 3) `int a = 1, b = 2;` NO
↓ keep ↓ id ↓ op ↓ id ↓

X 4) `String s = "Hello";` NO
→ No operator, Not punctuation, No regular

X 5) `char a = 'ab';` character automatically give error

X 6) `char b = 'ab';`

X 7) `String j = compiler` " error

✓ 8) `int a = 908;` NO

✓ 9) `float c = 9.7;` NO

~~X~~ `float d = 9...8;` lexical error

11) `int i a, b;`

~~X~~ `int i a, b;` error
↑↑↑

(3) `int a, b;`

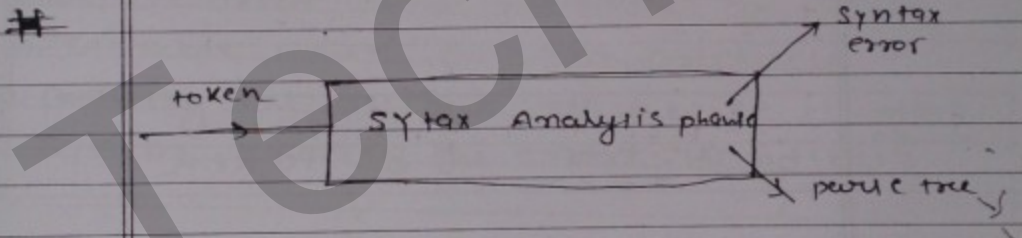
14) `Int a, b;` NO

No. of tokens1) int a, b, c; $\Rightarrow 7$ 2) printf ("compiler") ; $\Rightarrow 5$
1 2 3 4 53) printf ("%d %d", a, b) ; $\Rightarrow 9$
1 2 3 4 5 6 7 8 94) if (a > b)
{
a = b + c ;
} = 14 tokens5) ; a = b + c 6 tokens6) int findMax (int a, int b){if (a > b)return a ; $\Rightarrow 24$ A (Token)elsereturn b ;}

```
#
main()
{
    for(i=0; i<=10; i++)
}
```

compiler response for this code

- 1) lexical error: [FRO identifier]
- 2) ~~2) syntax error~~
- 3) lexical and syntax
- 4) None of these.



Syntax errors

- 1) Lack of tokens to frame Statement
- 2) More no. of token than actually required for a Statement
- 3)

$$\# \quad a = b + c * d$$

$$S \rightarrow id = E$$

~~$$E \rightarrow E + E \mid E * E \mid id$$~~

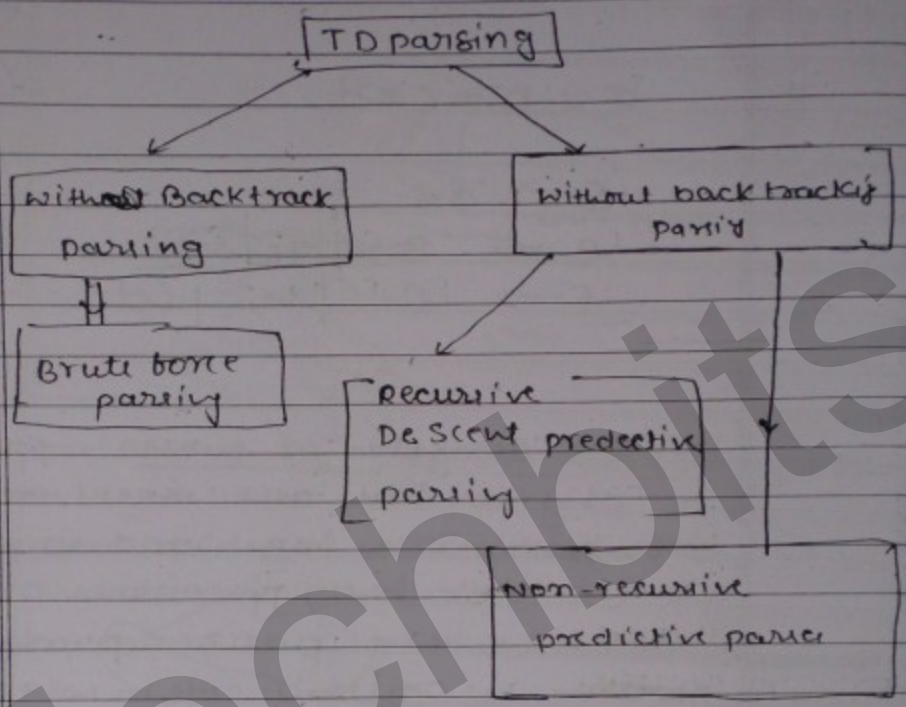
$$E \rightarrow E + E \mid E * E \mid id$$

Syntax analyzer or parser:- parser is a program, that takes tokens and context free grammar as input and verifies tokens are derivable from grammar or not. If derivable, then parser produces parse tree as output otherwise it writes syntax errors to the error handler.

The parsing can be done is top down, bottom up approach.

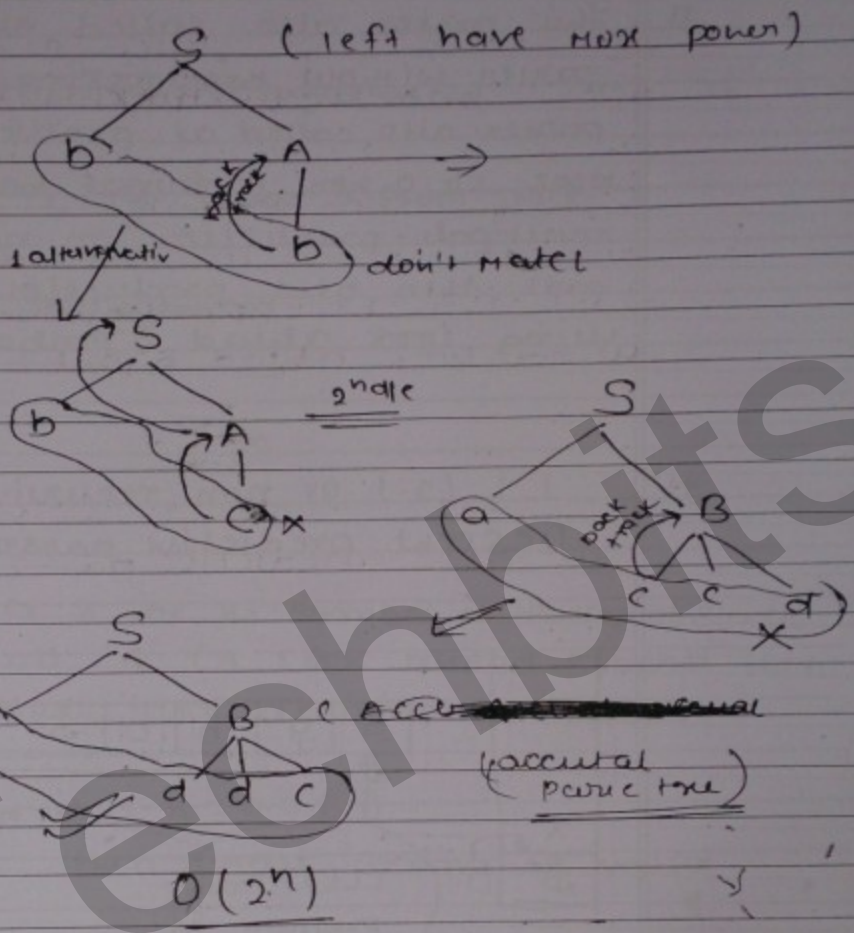
If any parser use top down parsing technique then it follows left most derivation in the construction of parse tree.

If any parser use bottom up parser technique then it use, reverse of right most derivation in construction of parse tree.

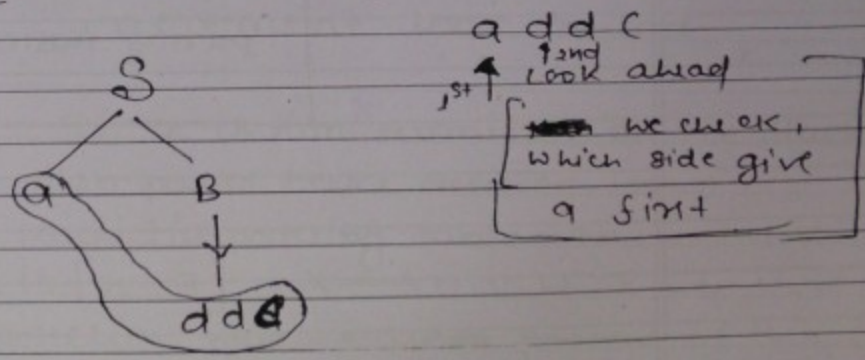


Q1

addc
 $S \rightarrow bA \mid aB$
 $A \rightarrow b \mid c$
 $B \rightarrow cd \mid ddC$

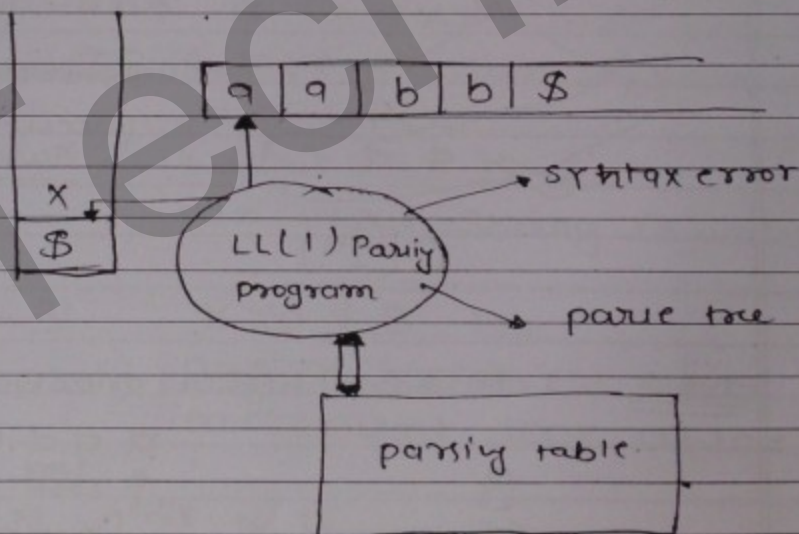


NOTE left have higher priority



#1 This parser also called as predictive parser. without backtracking topdown - parser also called as predictive parser. becoz it's a non terminal having, - multiple production on right hand - part then best production is selected using look ahead symbol.

#1 LL(1) or non recursive ~~parser~~ Descent predictive parser



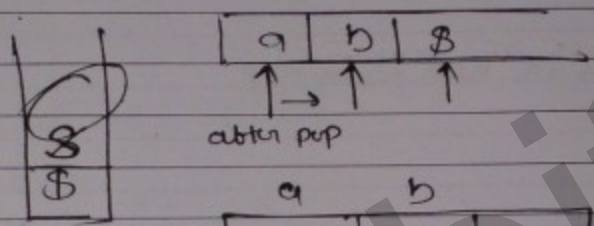
if

- 1) $x = a = \beta$ } input valid
- 2) $x = a \neq \beta$ } pop x from stack
- 3) x is non terminal

Let x be the symbol at the top of stack and 'a' is look ahead symbol then parser take decision as follows:

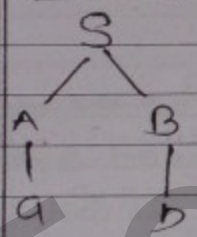
- 1) if $(x = a = \beta)$
then input string is valid
- 2) $x = a \neq \beta$ then
pop x from the stack
increment look ahead.
- 3) If x is non terminal on the stack
then parser take decision from -
predictive parsing table. In the table:
if $[x, a] : X \rightarrow u, v, w$ x was uvw
production such uvw present at then
replace x such the u appear at the
top of stack.

$[x, a]$ = blank entry in the table then there is syntax error, and written it do error handler.

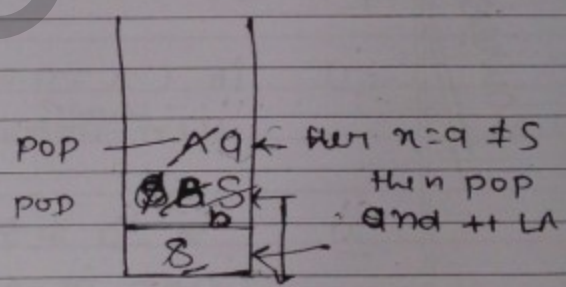


algo

making with S



	a	b	
S	S → AB		
A	A → a		
B		B → b	



x

$x = b \neq \$$



or

construction of LL(1) parsing table for the following grammar. And verify grammar is LL(1) grammar or not. also check whether it is ambiguous or not.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid \epsilon$$

$$F \rightarrow id$$

Size of table = (No. of non-terminal) \times (Terminal + Termind)

First and Follow

$$F = \{id\}$$

$$T' = \{*, \epsilon\}$$

$$T = \{id\}$$

$$F = \{id\}$$

$$E' = \{+, \epsilon\}$$

Follow E

$$E = \{\$ \}$$

$$E' = \{\$ \}$$

$$T' = \{+, \$ \}$$

$$T$$

$$F$$

	id	+	*	^	\$
E	$E \rightarrow TE'$				
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$				
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$
F	$F \rightarrow id$				

ii) All LL(1) grammar are unambiguous grammar. But all unambiguous grammar need not be LL(1)

Follow = $S = a$
 $A = a$
 $B = \{a, \epsilon\}$
 $C = \{b, \epsilon\}$

$$S \rightarrow a \textcircled{A} \textcircled{B} c$$

$$A \rightarrow a | bb$$

$$B \rightarrow a | \epsilon = \{a, \epsilon\}$$

$$C \rightarrow b | \epsilon = \{b, \epsilon\}$$

- | | |
|-----------------------|-----------------------|
| Final | Follow |
| $S = \{a\}$ | $S = \{\$ \}$ |
| $A = \{a, b\}$ | $A = \{a, b\}$ |
| $B = \{a, \epsilon\}$ | $B = \{a, \epsilon\}$ |
| $C = \{b, \epsilon\}$ | $C = \{b, \epsilon\}$ |

Construct LL1 parsing table for the following grammar

- $S \rightarrow aABC$
- $A \rightarrow a | bb$
- $B \rightarrow a | \epsilon$
- $C \rightarrow b | \epsilon$

[For, ϵ calculate follow then choose position where to place.]

	a	b	ϵ
S	$S \rightarrow aABC$		
A	$A \rightarrow a$	$A \rightarrow bb$	
B	$B \rightarrow a$	$B \rightarrow \epsilon$	$B \rightarrow \epsilon$
C		$C \rightarrow b$	$C \rightarrow \epsilon$

$S \rightarrow a @ \underline{B} E$
 $A \rightarrow \underline{A} B C / b$
 $B \rightarrow \underline{d}$

first

follow

$S = \{a\}$
 $A = \{b\}$
 $B = \{d\}$

$S = \{\$ \}$
 $A = \{d\}b\}$
 $B = \{ \}$

	a	b	c	d	e	\$
S	$S \rightarrow a @ \underline{B} E$					
A		$A \rightarrow \underline{A} B C$ $A \rightarrow b$				
B				$B \rightarrow d$		

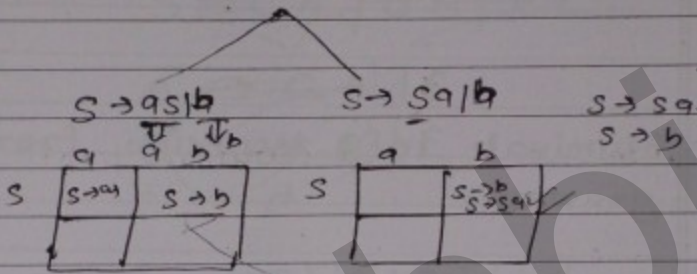
NOTE

#

If grammar contain Left recursion then there is multiple entry in table.

NOTE

power of parser :- The number of grammar handled by a particular parser, is known as power of that parser.



NOTE :- If a grammar contain left-recursion then its predictive parsing table contain multiple entries. Hence left recursive grammar are not LL(1).

∴ We can make this grammar are LL(1) by removing, left recursion for that.

Removing of left recursion

$S \rightarrow S a / b$
 generated string = $b a^*$
 Removed

∴ $S \rightarrow b S'$ = b } there is
 $S' \rightarrow a S' / \epsilon = a^*$ } no more
 = $b a^*$ } left recursive

#1

$$A \rightarrow A\alpha_1 | A\alpha_2 \quad \text{---} \quad \left\{ B_1 | B_2 | B_3 \right\} \quad \text{---}$$

$$A \rightarrow B_1 A' | B_2 A' | B_3 A' \quad \text{---}$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \dots \alpha_n A' \dots$$

#1

Eliminate left recursion from -
grammar.

$$E \rightarrow E + T | T$$

$$T \rightarrow T * F | F$$

$$F \rightarrow id$$

 \Rightarrow

$$E \rightarrow T A'$$

$$A' \rightarrow \epsilon + ET | \epsilon$$

$$T \rightarrow F B'$$

$$B' \rightarrow * FT | \epsilon$$

$$F \rightarrow id$$

Removed
left recursion

Eliminate left recursion form following gsm

$$S \rightarrow Sa | Sb | c | d | e$$

$$S \rightarrow cA' | dB' | eC'$$

$$A' \rightarrow aA' | \epsilon$$

$$B' \rightarrow dB' | \epsilon$$

$$C' \rightarrow e$$

$$S \rightarrow cS' | dS' | eS'$$

$$S' \rightarrow aS' | bS' | \epsilon$$

More problem

#

$$S \rightarrow aB | aA \quad \{ \text{string } ab \}$$

$$A \rightarrow a | b \quad \{ \text{ambiguous this problem} \}$$

$$B \rightarrow d | c \quad \text{create problem for LL(1)}$$

↓

Solⁿ :- using left factoring we remove ambiguity problem.

$$S \rightarrow aB | aA$$

$$A \rightarrow a | b \quad \Rightarrow$$

$$B \rightarrow d | c$$

$$S \rightarrow a(B+A) \Rightarrow S \rightarrow aZ'$$

$$Z' \rightarrow B | A$$

$$A \rightarrow a | b$$

$$B \rightarrow d | c$$

Removed ambiguity.

$$\# \quad A \rightarrow \alpha B_1 | \alpha B_2 | \alpha B_3 | \dots | \alpha B_n$$

$$A \rightarrow \alpha B$$

$$B \rightarrow B_1 | B_2 | \dots | B_n$$

left factor the grammar

$$S \rightarrow iEtS | iEtSes | a$$

$$E \rightarrow b$$

$$\therefore S \rightarrow iEtS (EtS) | a$$

$$S \rightarrow iEtS z' | a \quad \checkmark$$

$$z' \rightarrow EtS'$$

$$E \rightarrow b$$

NOTE GATE prob

It is impossible to convert into LL(1) grammar

Done
*
#

$S \rightarrow AB \checkmark$
 $A \rightarrow a \checkmark$
 $B \rightarrow b \checkmark$

} single production

LL(1)

Q1

 $S \rightarrow aABe$
 $A \rightarrow \underline{ABC}/b$ (left recursion)

 $B \rightarrow d$

Not LL(1)

#

 $S \rightarrow ab|aqa$

common prefix so Not LL(1).

#

 $\checkmark S \rightarrow AB$
 $\checkmark A \rightarrow a/b$ [cannot fix + of a, b]

 $\checkmark B \rightarrow b/c$ [i.e. a, b]

and Λ is ϕ so LL(1)

$$\begin{aligned}
 E &\rightarrow TE' \quad \checkmark \quad \text{S.P} \\
 E' &\rightarrow +TE' \mid id \quad \left\{ \begin{array}{l} \text{first of } +TE' \text{ is } + \\ \text{first of } id \text{ is } id \end{array} \right. \\
 T &\rightarrow FT' \quad \checkmark \quad \text{S.P} \\
 T' &\rightarrow *FT' \mid \epsilon \Rightarrow \text{calculate Follow } T' \\
 F &\rightarrow id \quad \checkmark \quad \text{S.P} \quad \text{ie}
 \end{aligned}$$

#1

$$S \rightarrow aSA \mid \epsilon$$

$$A \rightarrow \underline{c} \mid \underline{\epsilon} \rightarrow \text{first}(a) \quad \downarrow \text{for this calculate follow of } S$$

$$\begin{aligned}
 S \Rightarrow \text{first } A \{c, \epsilon\} \text{ then remove } A \Rightarrow \\
 \{c, \phi\} \cap \text{first}(aSA) = \phi
 \end{aligned}$$

$$\begin{aligned}
 \text{first of } (c) = c \quad n \neq \phi \text{ then} \\
 \text{follow } (A) = \{c, \phi\} \\
 \underline{\text{NOT LL (1)}}
 \end{aligned}$$

#1

$$E \rightarrow TE'$$

$$E' \rightarrow +T$$

#

$$S \rightarrow a \underline{S} a \mid \underline{\epsilon} \quad \{c, \epsilon, \$\}$$

$$A \rightarrow \underline{c} \mid \underline{\epsilon}$$

S

Q1

$$S \rightarrow a \underline{S} b \mid b \underline{S} a \mid \underline{\epsilon}$$

Q2

$$[S, a] \Rightarrow$$

follow S = (b, a, \$)

Not LL(1) = A

$$[S, a] \Rightarrow a S b S$$

$$[S, a] = S \rightarrow \epsilon$$

$$[S, b] = S \rightarrow b S a S$$

$$[S, b] = S \rightarrow \epsilon$$

consider the following grammar,

$$\begin{aligned}
 S &\rightarrow i \mid t \mid SS \\
 S &\rightarrow e \mid E \\
 E &\rightarrow b
 \end{aligned}$$

predictive parsing table entries (S', E)
(S', e)

follow

Q1 consider following grammar and predictive parsing table.

$$\begin{aligned}
 S &\rightarrow aAbB \mid bAaB \mid E \\
 A &\rightarrow S \mid b \\
 B &\rightarrow S
 \end{aligned}$$

	a	b	\$
S	$S \rightarrow E$ $S \rightarrow aAbB$	$S \rightarrow E$ $S \rightarrow bAaB$	$S \rightarrow E$
A	$A \rightarrow S$	$A \rightarrow S$	
B	$B \rightarrow S$	$B \rightarrow S$	$B \rightarrow S$

First =

~~First = $\{a, b, \epsilon\}$~~

Follow $\rightarrow S \rightarrow A \rightarrow b$

Follow $\rightarrow B \rightarrow$

First(ϵ) = $\{a, b, \epsilon\}$ | Follow(ϵ) = $\{\$, \epsilon\}$

First(A) \rightarrow First(S) $\Rightarrow \{a, b, \epsilon\}$ for ϵ

Follow(A) $\Rightarrow \{\$, a\}$ ✓

First(B) $\Rightarrow \{a, b, \epsilon\}$

Follow(B) $\Rightarrow \{\$, a, b, \epsilon\}$ ✓

#1

$S \rightarrow AB$

$A \rightarrow aa|ab$

$B \rightarrow ba|bb$

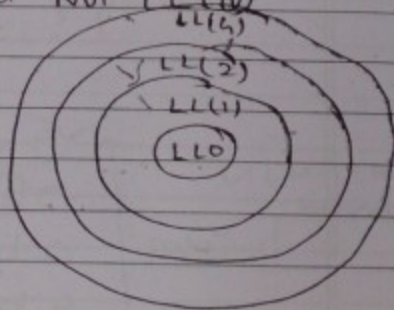
LL(1) but Not LL(0)

#1

$S \rightarrow AB$

$A \rightarrow a|b$

$B \rightarrow b|a$



#1

$S \rightarrow AB$

$A \rightarrow a$

$B \rightarrow b$

NOTE:- All LL(k) grammars are unambiguous but all unambiguous grammars need not be LL(k) where k is the length of look ahead

01) Consider the following grammar

$$S \rightarrow ER \quad (S, id)$$

$$R \rightarrow *S \mid \underline{\epsilon} \quad (*, id)$$

$$E \rightarrow \underline{id}$$

in predictive parsing table to enter

$$[S, id] [R, \epsilon] \checkmark$$

$$\downarrow [R,$$

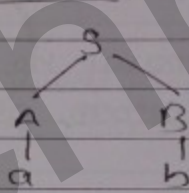
$$[R]) (R \rightarrow \epsilon) \checkmark$$

NOTE

Top down parser can't work for, left recursive grammar and non deterministic grammar. Even if eliminate the, left recursion from the grammar (order precedence, and associativity rules and readability also. Hence we need a parsing technique that can for "left recursive grammar" i.e Bottom up parsing.

$S \rightarrow AB$
 $A \rightarrow a$
 $B \rightarrow b$

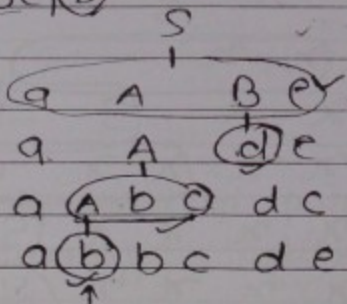
ab string



11

$S \rightarrow aABe$
 $A \rightarrow ABC|b$
 $B \rightarrow d$

abbcde

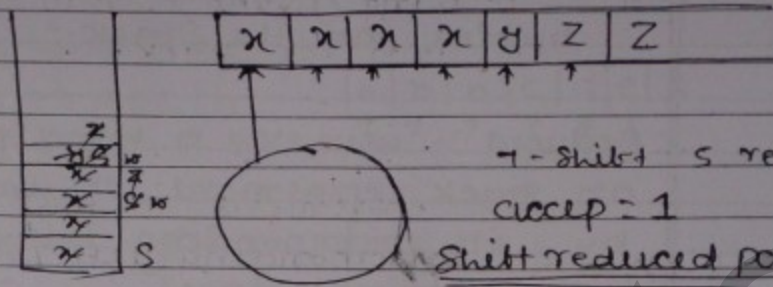
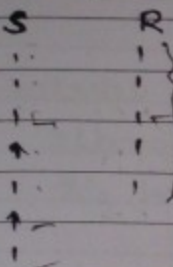


✓ (mark are) handles

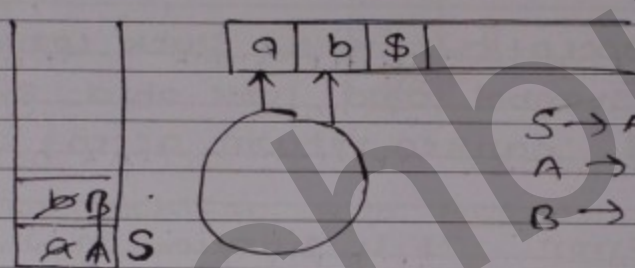
↑ parsing

NOTE Bottom up parser construct the parse tree starting from, giving string and proceeds until, starting symbol of grammar.

Q2)

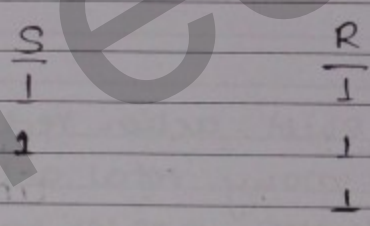


- Shift + S reduced
 accept = 1
Shift reduced parser



S → AB
 A → a
 B → b

Stack



All the bottom up parser will work based on following 4 action

- 1) Shift
- 2) reduce
- 3) accept
- 4) error

Shift :- pushing symbol from input buffer into the stack.

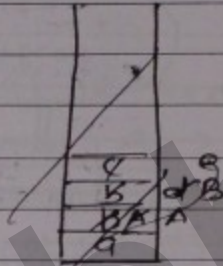
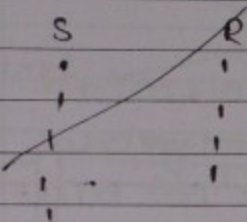
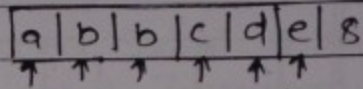
Reduced :- whenever a handle is detected on stack replacement of that handle by its corresponding left hand is non terminal done.

accept :- with the stack contain starting symbol and look ahead symbol is "\$" parser return accept action.

Error :- It is situation in which parser can't apply either shift action or reduced action not even accept also.

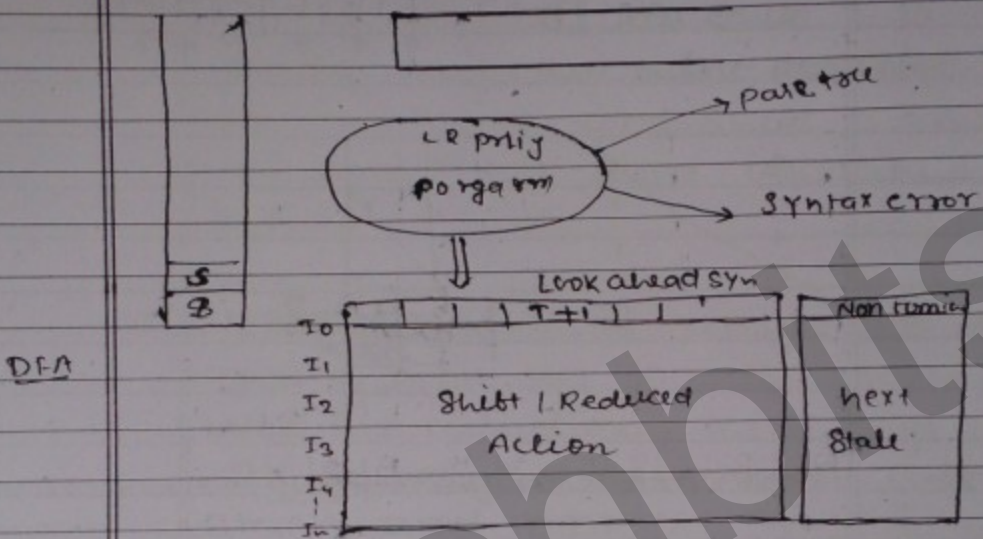
Q1 How many shift action reduced action How many total action taken by shift reduced parser to parse

$$\left. \begin{array}{l} \text{Shift} = 7 \\ \text{Reduced} = 5 \\ \text{accept} = 1 \end{array} \right\} = 13 \quad 02A$$

$S \rightarrow a A B e$
 $A \rightarrow A B C / b$
 $B \rightarrow d$


Two problem with LR

- 1) Reduced Reduced @ conflict
- 2) when to do reduced and , shift

LR parsing

- 1) Let S be the state on the top of stack "a" is the look ahead symbol then parser take decision regarding shift reduced action from the parsing table.
- ⇒ following are the possible action in the parsing table

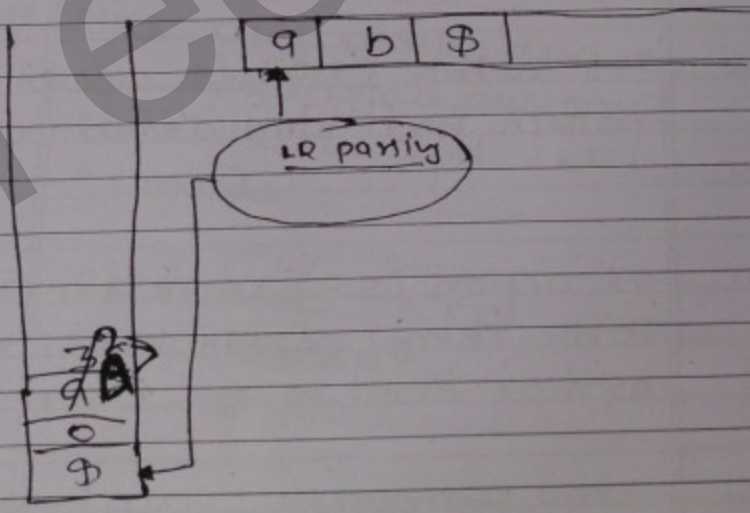
- # If action $[s, a]$ is 'Shift' in the parsing table, then shift ~~symbol~~ 'a' into the stack and shift j on the top onto stack and increment look ahead symbol.
- # If action $[s, a]$ is 'reduce' in the parsing table and $A \rightarrow B$ is the production used for reduction, then pop $2 \times |B|$ (length of B) symbols from the stack and push 'A' onto the stack and then push goto (i, A) onto the top of stack where 'i' is previous state onto the stack.
- 5' If action $[s, a]$ is 'accept' and stop parser halt and announce success.
- # If action $[s, a]$ is 'error' (blank in the table entry) parser halt, return syntax error to the error handler.
- # Time complexity = $O(n)$ where n is length of input string.

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Date: / /

	ACTION			goto		
	a	b	B	S	A	B
r_0	S_3		accept	1	2	
r_1						
r_2		S_5				4
r_3		r_2				
r_4			r_1			
r_5			r_3			
r_6						
r_7						
r_8						

$S \rightarrow AB$
 $A \rightarrow a$
 $B \rightarrow b$



Stack	input buffer	Action
\$ 0	a b \$	$[0, a] = \text{shift } 3$
\$ 0 a 3	a b \$	$[3, b] = \text{Reduce } (A \rightarrow a)$
\$ 0 A 2	a b \$	$[2, b] = \text{shift } 5$
\$ 0 A 2 (b) 5	\$	$[5, b] = \text{Reduce } B \rightarrow b$
\$ 0 A 2 B 4	\$	$[4, B] = \text{Reduce } S \rightarrow AB$
\$ 0 S 1	\$	$[1, S] = \text{Accept}$

Note any parser derived on table known as table driven parser.

Since LL(1) and LR(1) parsers are examples

Recursive descent parser is not table driven.

#1

How many reduced action how many shift and total action taken by LR process to parse input string (iti) by considering following parse table.

$$E \rightarrow T+E$$

$$E \rightarrow T$$

$$T \rightarrow i$$

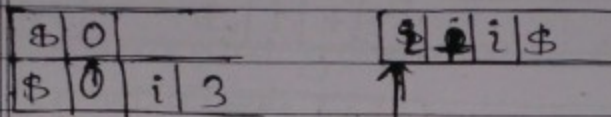
	i	+	\$	E	T
I ₀	S ₃		accept	1	2
I ₁					
I ₂		S ₄	r ₂		
I ₃		r ₃	r ₃		
I ₄	S ₃			5	2
I ₅			r ₁		

0
\$

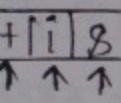
Stack

Input buffer

Action



~~S0~~



S0

S0 i 3

$[0, i] = S_3$

S0 i 3 Φ

$[3, T] = R_3 \text{ (T} \rightarrow \text{i)}$

S0 i T 2 + 4

$[2, T] = S_4$

S0 i T 2 + 4

$[4, i] = S_3$

S0 i T 2 + 4 (i 3)

$[3, \Phi] = \gamma_3 \text{ T} \rightarrow \text{i}$

S0 i T 2 + 4 (T 2)

$[2, \Phi] = \gamma_2 \text{ E} \rightarrow \text{T}$

S0 i T 2 + 4 E 5

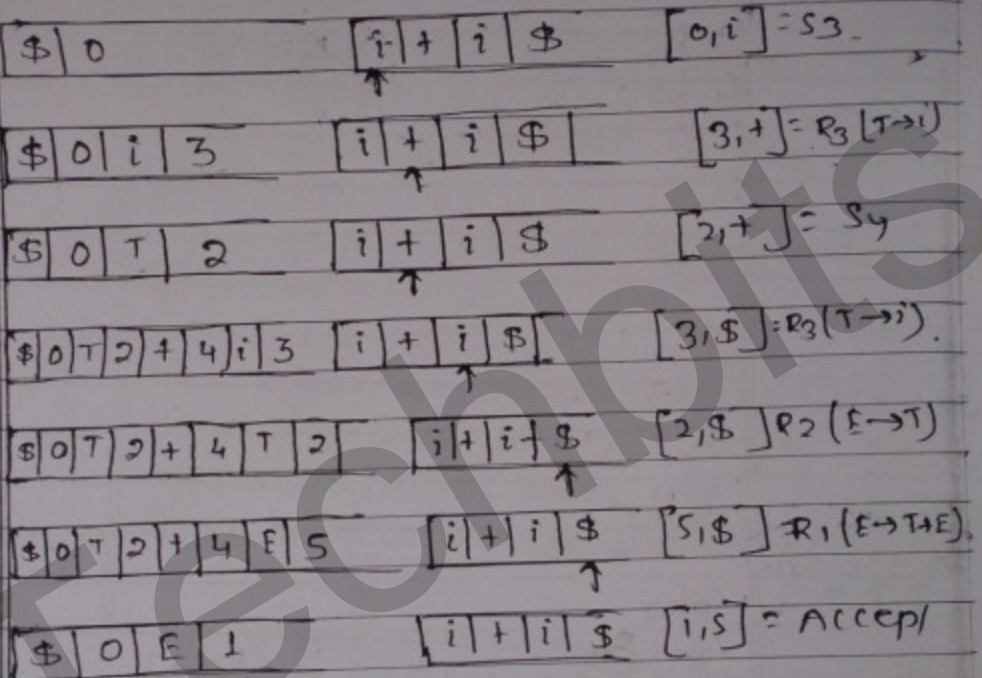
$[5, \Phi] = \gamma_1 \text{ E} \rightarrow \text{T+E}$

~~S0 i T 2 +~~

S0 i

Stack

input buffer



construction of LR(0) parsing table

- 1) Augmented grammar:- Adding a New production

$S' \rightarrow S$ to the original grammar.

- 2) This augmented production helps the parser to show accept action i.e. whenever parser tries to reduce S by S' it lead to accept action.

- 3) compute LR(0) item:-

LR(0) item is nothing but a context free grammar production having a "." on the RHS part.

$A \rightarrow \cdot XYZ$ parser has seen 'x'

$A \rightarrow \widehat{X} \cdot YZ$ and ready to see "yz".

$A \rightarrow \widehat{XY} \cdot Z$

$A \rightarrow \widehat{XYZ} \cdot$

$S' \rightarrow \cdot S$ (parser ready to see right hand side part)

closure $S' \rightarrow \cdot S$
 $S \rightarrow \cdot AB$
 $A \rightarrow \cdot a$

It goto mean's move " \cdot " 1 more right place.

closure :- closure function add non terminal ~~to~~ production and it will put " \cdot " on right hand part of the production.

note :- goto function move " \cdot " 1 position ahead.

a) construct LR(0) parsing table, for the following grammar. And verify grammar is LR(0) or not. check it is ambiguous or, unambiguous.

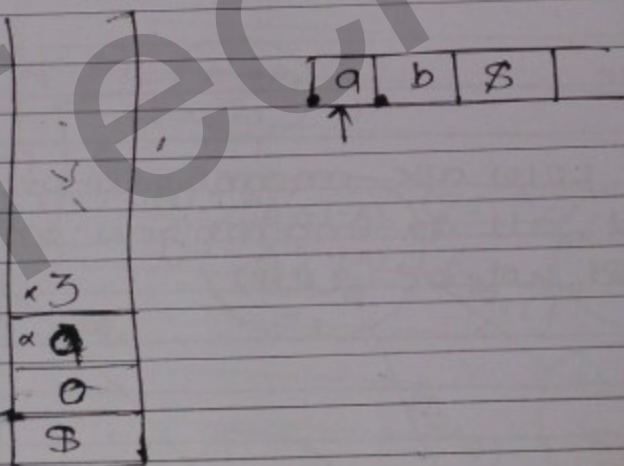
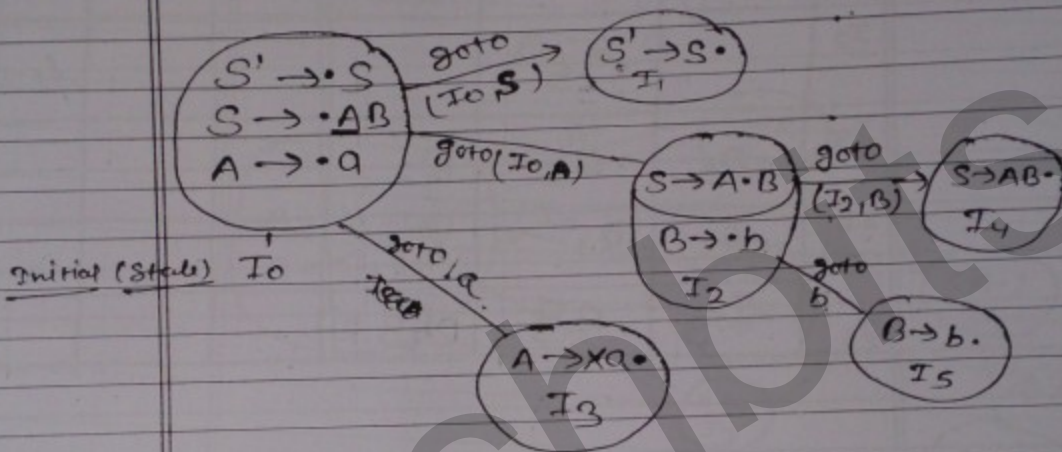
Ans

$S \rightarrow AB$
 $A \rightarrow a$
 $B \rightarrow b$

Construct
 augmented
 grammar

Accept $S \rightarrow S!$

$R_1 S' \rightarrow AB$
 $R_2 A \rightarrow a$
 $R_3 B \rightarrow b$



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Shift

	a	b	S	A	B
I ₀	S ₃		1	2	
I ₁			Accept		
I ₂		S ₅			4
I ₃	R ₂	R ₂	R ₂		
I ₄	R ₁	R ₁	R ₁		
I ₅	R ₃	R ₃	R ₃		

Note

All LR(0) are unambiguous grammar
 but all unambiguous grammar
 need not be LR(0)

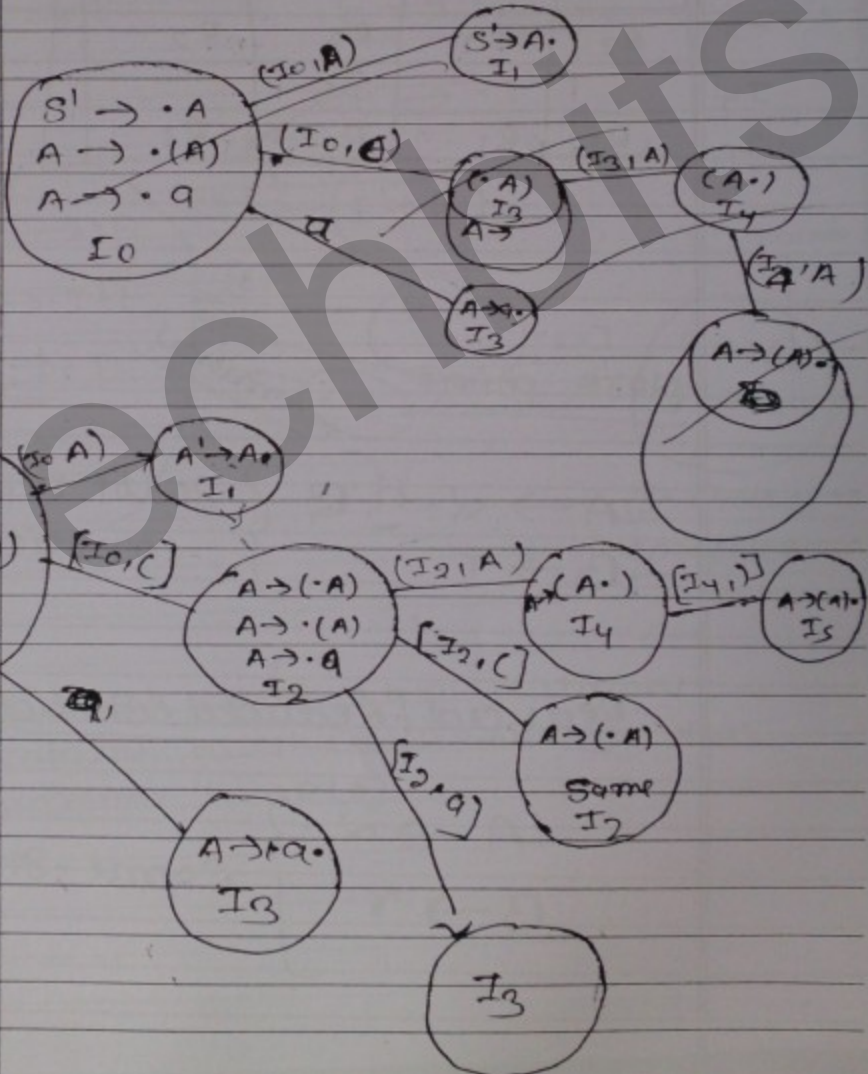
Q1

$A \rightarrow (A)$

$A \rightarrow \epsilon$



$S' \rightarrow A$
 $A \rightarrow (A)$
 $A \rightarrow \epsilon$



	a	c)	\$	A
I ₀	S ₃	S ₂			1
I ₁					
I ₂	S ₃	S ₂			4
I ₃	R ₂	R ₂	R ₂	R ₂	
I ₄			S ₅		
I ₅	R ₁	R ₁	R ₁	R ₁	

NOTE point

terminal

LR(0)

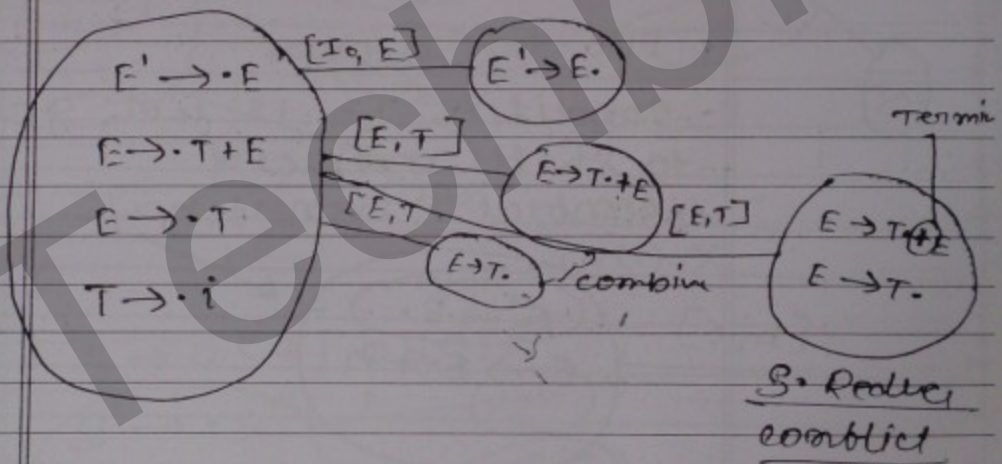
$A \rightarrow \alpha \cdot \underline{a} B$
 $B \rightarrow \gamma \cdot$

} shift reduced,
conflict

Reduced / Reduced conflict

$A \rightarrow \alpha \cdot$
 $B \rightarrow \gamma \cdot$

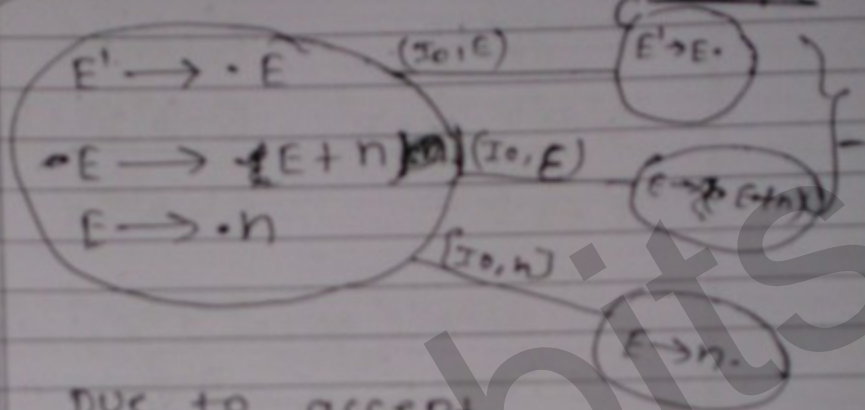
} same state

~~$E' \rightarrow E$~~ $E \rightarrow T + E$ $E' \rightarrow \cdot E$ $E \rightarrow T$ \Rightarrow $E \rightarrow \cdot T + E$ $T \rightarrow i$ $E \rightarrow \cdot T$ $T \rightarrow \cdot i$ 

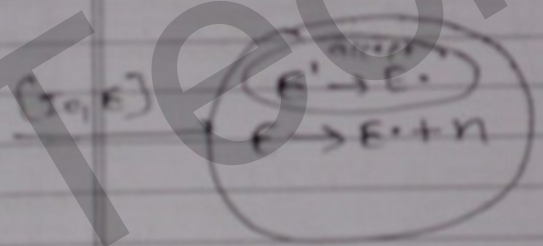
Note:- If LR(0) item automata contains atleast inadequate sets then the grammar is LR(0)

GATE

$$E \rightarrow E + n \mid n$$



DUE to accept condition it is not going to shift reduced conflict even if now



01

check whether following grammar is LR(0) or not.

$$E \rightarrow E+T$$

$$E' \rightarrow \cdot E$$

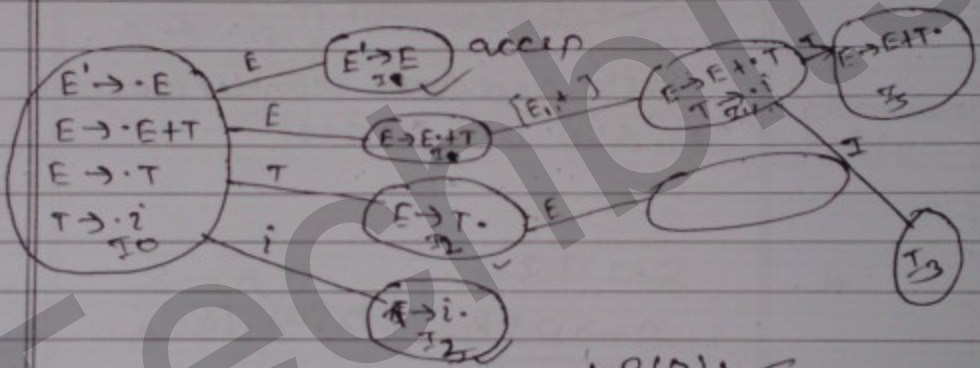
$$E \rightarrow T$$

$$\Rightarrow E \rightarrow \cdot E+T$$

$$E \rightarrow \cdot T$$

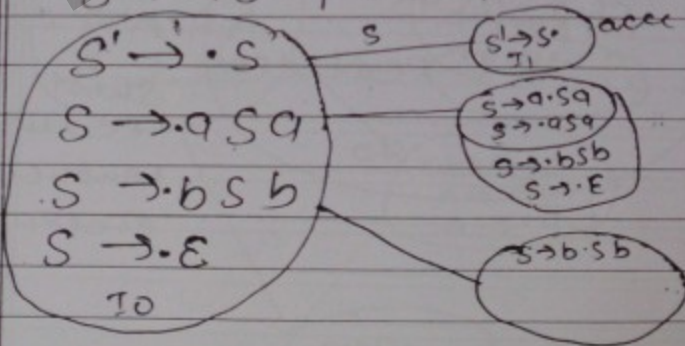
$$T \rightarrow i$$

$$T \rightarrow \cdot i$$



11

$$S \rightarrow aSa | bSb | \epsilon$$



#

 $S \rightarrow aSa \mid bSb \mid \epsilon$

$S' \rightarrow \cdot S$
 $S \rightarrow \cdot aSa$
 $S \rightarrow \cdot bSb$
 $S \rightarrow \epsilon \{ \text{Reduce} \}$
 To

Shift reduced conflict occurs
 so it is not LR(0)

#

 $S \rightarrow aSbS$ $S \rightarrow aSbS \mid bSaS \mid \epsilon$

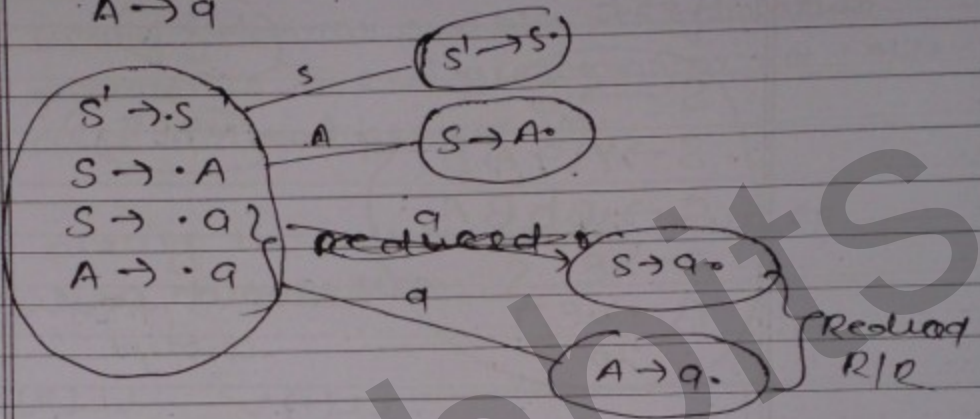
$S' \rightarrow \cdot S$
 $S \rightarrow \cdot aSbS$
 $S \rightarrow \cdot bSaS$
 $S \rightarrow \cdot \epsilon \{ \text{Reduced} \}$
 To

Not LR(0)

Shift
 Reduced
 conflict
 occur.

$S \rightarrow A|q$

$A \rightarrow q$

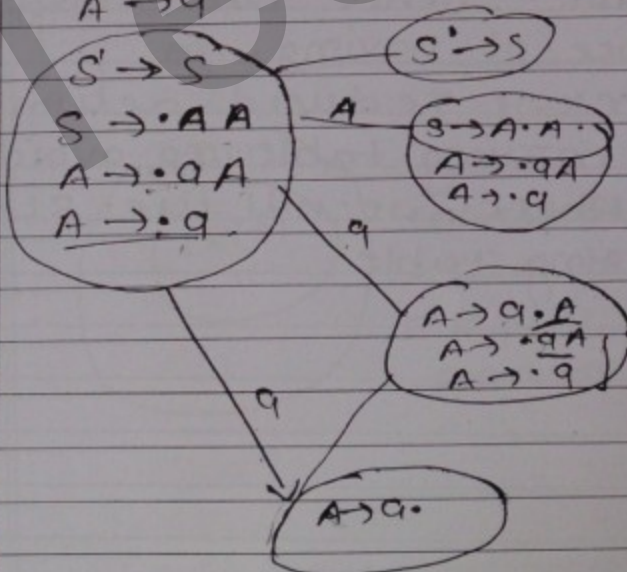


Q1

$S \rightarrow A A$

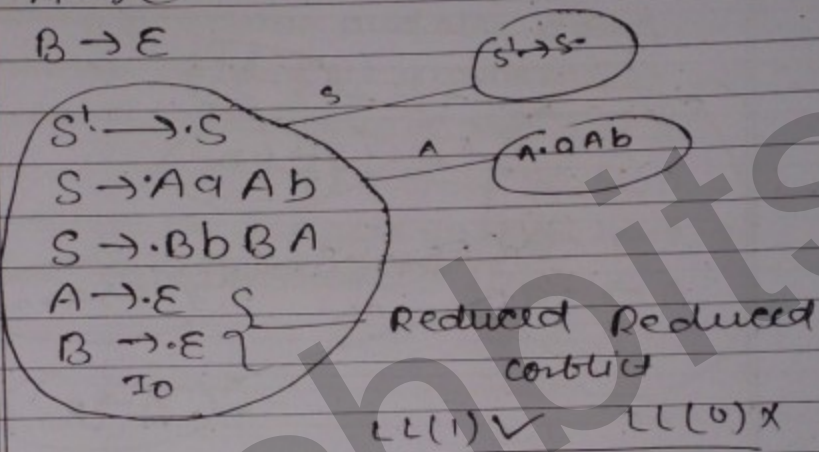
$A \rightarrow q A$

$A \rightarrow q$



$$S \rightarrow AaAb \mid BbBa$$

$$A \rightarrow \epsilon$$

$$B \rightarrow \epsilon$$


NOTE :- In LR(0) "0" indicate no look ahead concept is used to place the reduced action. Hence there may be chance of having unnecessary reduced action in the parsing table. To avoid this drawback, we will use SLR(1) parsing table.

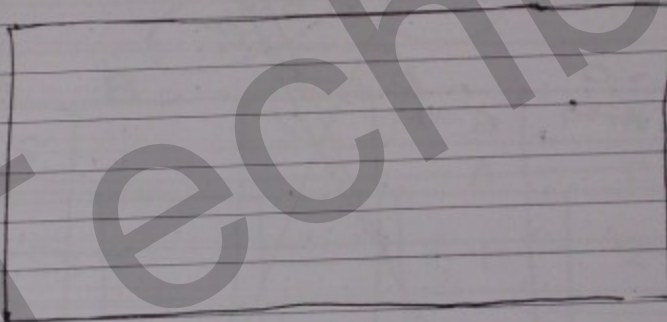
SLR(1) = simple LR(1)

construct SLR(1) parsing table for the following grammar and also verify whether grammar is SLR(1) grammar or not. Also check it ambiguous or not.

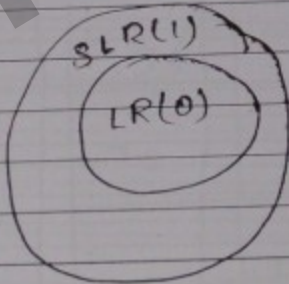
As

placing the reduced entry base on above calculation.

I_0
 I_1
 I_2
 I_3
 I_4
 I_5



#

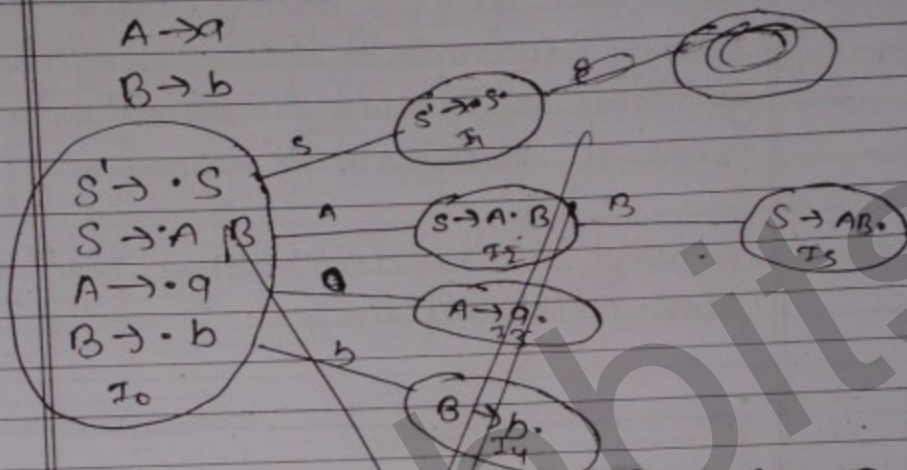


power SLR(1) > power LR(0)

and it is unambiguous grammar.

Q1) Check whether grammar is SLR(1)

Q. $S \rightarrow AB$
 $A \rightarrow a$
 $B \rightarrow b$

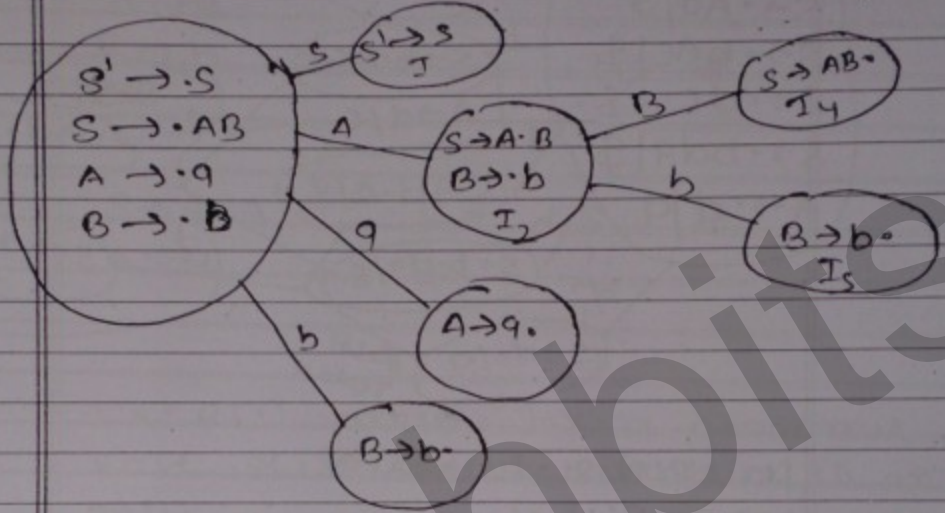


	a	b	\$	S	A	B
I ₀	A → a	B → b			2	3
I ₁						
I ₂						5
I ₃						
I ₄						
I ₅						

$S \rightarrow AB$

$A \rightarrow a$

$B \rightarrow b$



	a	b	S	A	B	.
I_0	S_3			1	2	
I_1						
I_2		S_5			4	
I_3		r_2		.		
I_4			r_4			
I_5			r_3			

①)

 $S \rightarrow AqAb$ $S \rightarrow BbBq$ $A \rightarrow a$ $B \rightarrow b$ check for LR(1) #

±1

 $S \rightarrow A/a$ $A \rightarrow a$ $\Rightarrow \begin{array}{c} S \\ | \\ a \end{array}$ $\Rightarrow \begin{array}{c} S \\ | \\ A \\ | \\ a \end{array}$

②)

LALR(1) parser, for a grammar have shift reduce conflict, it an only.

1) LR(1) grammar reduce reduce conflict

2) LR(0) grammar have reduce reduce conflict

3) LR(1) have shift reduce

4) Non of this

Q) Consider the following grammar and following

$$S \rightarrow S * E$$

$$S \rightarrow E$$

$$E \rightarrow F + E$$

$$E \rightarrow F$$

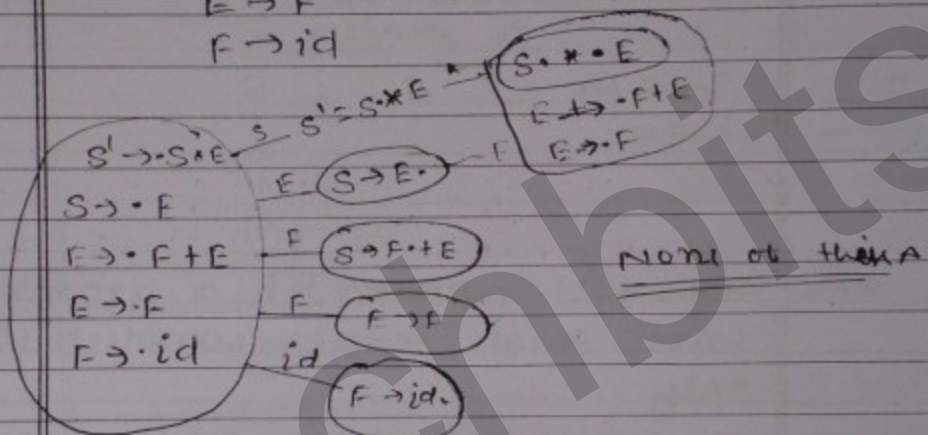
$$F \rightarrow id$$

LR(0) items

1) $S \rightarrow S * E$

2) $E \rightarrow F + E$

3) $E \rightarrow F$



Q) Consider the following grammar which of following is

$$S \rightarrow CC$$

$$C \rightarrow c C / a$$

1) This is LL(1)

2) This is LR(1) but not LL(1)

3) This is LL(1) but not LALR(1)

4) This is neither

Q1) condense the following grammar

$$E \rightarrow E + n \mid E * n \mid n$$

which of the following are the handle in the right sentential form.

A $n + n * n$

$$\begin{array}{l} \underline{E} \\ \underline{E} \quad \underline{*n} \\ \underline{E + n * n} \\ \underline{n + n * n} \end{array}$$

handle $\{E + n, E * n\}$

Q1

	LR(0)	SLR(1)	CLR(1) and LALR(1)
Shift/Reduce	$A \rightarrow \alpha a B$ $B \rightarrow \gamma$	$A \rightarrow \alpha \overset{\text{a}}{\text{B}}$ $B \rightarrow \gamma$ $\text{follow}(B) = \{ \gamma \}$	$A \rightarrow \alpha a B$ $B \rightarrow \gamma \{ \downarrow \}$ $\text{fb} = a = \{ \downarrow \}$
Reduce/Reduce	$A \rightarrow \alpha$ $A \rightarrow \gamma$ $A \rightarrow B$	$A \rightarrow \alpha$ $B \rightarrow \gamma$ $\text{follow}(A) \cap \text{follow}(B) \neq \phi$	$A \rightarrow \alpha, \{ \downarrow \}$ $B \rightarrow \gamma, \{ \downarrow \}$ $\text{follow}(A) \cap \text{follow}(B) \neq \phi$

LR(1) by default CLR(1)

NOTE - If we remove the ambiguity from the grammar, lower readability.

Removal of ambiguity is not advisable. Hence to handle ambiguous grammar, the suitable parsing technique is operator parsing.

Operator precedence parsing

- 1) Ambiguous grammar and unambiguous
 - 2) Simple to design.
- > we can construct operator precedence parsing for the operator precedence grammar

operator precedence grammar is not LL1 but operator grammar having at most one precedence-relation b/w any pair of terminals.

operator grammar is not LL1 but context free grammar, no ϵ rule define and no adjacent variable on the right hand side part.

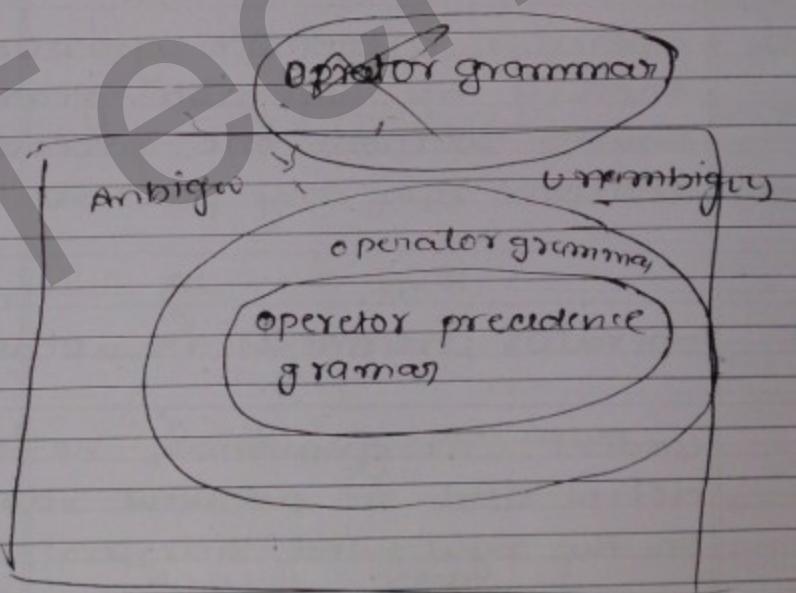
Q1

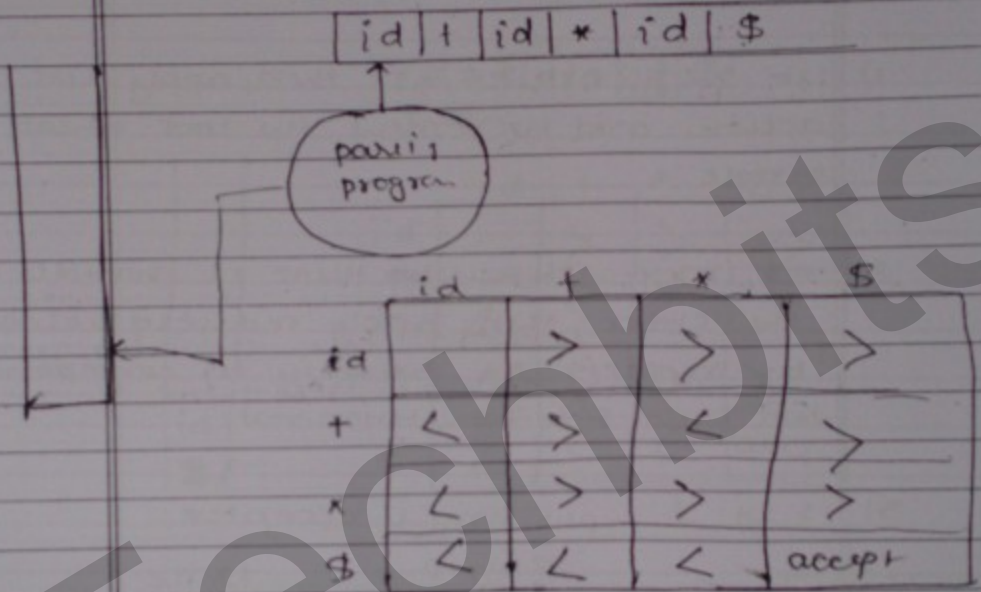
Which the following two rule, violate the requirement of operator grammar.

- 1) $P \rightarrow CaR$
- 2) $P \rightarrow E X$
- 3) $P \rightarrow C b R_1$
- 4) $P \rightarrow OR X$

#

Every operator precedence grammar is operator grammar but, operator grammar need not be operator precedence grammar.



operator precedence parser algo

operator precedence parser table

$$\begin{array}{l} x < y \\ x = y \end{array} \left. \vphantom{\begin{array}{l} x < y \\ x = y \end{array}} \right\} \text{shift}$$

$$x > y \left. \vphantom{x > y} \right\} \text{reduce action}$$

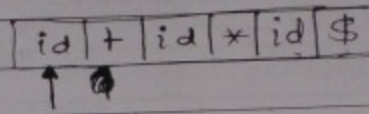
$$\begin{array}{l} x = y = \$ \text{ accept} \\ [x, y] = \text{blank} = \text{error} \end{array} \left. \vphantom{\begin{array}{l} x = y = \$ \text{ accept} \\ [x, y] = \text{blank} = \text{error} \end{array}} \right\}$$

Let 'x' is the top most, terminal on the stack, and 'y' is current look ahead symbol. then, parser will take action, based on the parsing table.

- 1) if $x < y$ or $x = y$ then, apply shift action and increment the look ahead single.
- 2) if $x > y$, then ~~to~~ there is handle in the stack, then apply reduced action by replacing the handle by correspondingly left hand side non terminal.
- 3) $x = y = \$$ input string is accepted.
- 4) if x and y blank entry in parsing table then there is syntax error written into error handle.

Q1 How many shift action, reduce action and how many total action taken by parser.

$$id + id * id$$



		id	+	*	\$
id	.	>	>	>	>
+	<	>	<	>	>
*	<	>	>	>	>
\$	<	<	<	acc	

Stack		Input str	Action
\$	↓	id + id * id	Shift
\$ id		id + id * id	Reduce
\$ E		id + id	Shift
\$ E +		id + id * id	Shift

Non-termining

+	
id	E
\$	

Construction of table.

Ambiguous:

$+ < *$

$* \equiv /$

$- < *$

$\uparrow > *$

Unambiguous grammars

1) $a = b$

$S \rightarrow \alpha a A b \beta$

2) $S \rightarrow \alpha a A B \beta$, $A < b$

$A \rightarrow \gamma b \delta$

3) $a > b$

$S \rightarrow \alpha A b \beta$

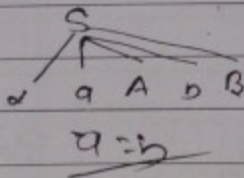
$A \rightarrow \gamma a \delta$

Note

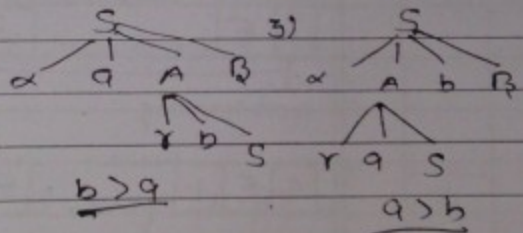
Dollen(\$) :- \downarrow is precedence.

Parse tree

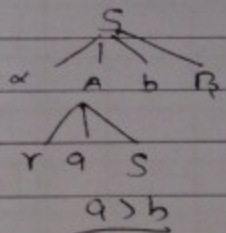
1)



2)



3)



If any operator grammar contains, both left recursion, or right recursion - it is ambiguous

If operators grammars contain either left recursion or right recursion every operator present at one non terminal only the grammar is unambiguous.

Grammar is unambiguous, parsing table is constructed based on the given grammar.

If the grammar is ambiguous, general programming language precedence use to construct parsing table.

Q1) Construct operator precedence table
 $A \rightarrow A * A / A + A | id$

Note

1) identifier is always highest precedence over the other operator

2) \$ is always lower precedence.

3) Identifier, identifier ~~is~~ precedence available
 $[id, id] \rightarrow \underline{no}$

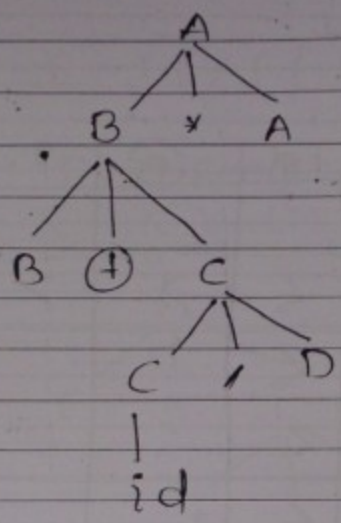
c) $[S, \$]$ is accep.

	id	+	*	\$
S		>	>	>
+	>	>	<	>
*	>	>	>	>
B	>	<	<	accep

01

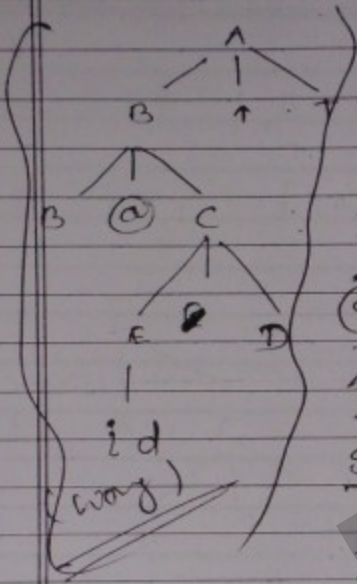
$A \rightarrow B * A \mid B$
 $B \rightarrow B + C \mid C$
 $C \rightarrow D \mid C \mid D$
 $D \rightarrow id$

	id	+	*	/	\$
id	>	>	>	>	>
+	<	>	>	<	>
*	<	<	<	<	>
/	<	>	>	>	>
\$	<	<	<	<	accept



- #1 $A \rightarrow B \uparrow T / B$
- $B \rightarrow B @ e / C$
- $C \rightarrow D \$ C / D$
- $D \rightarrow E - D / E$
- $E \rightarrow id$

	\uparrow	@	\$	\$
\uparrow				
@				
\uparrow				
\$				
\rightarrow				



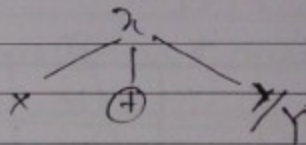
	id	@	↑	B	-	\$
id		>	>	>	>	>
@	<		>			>
↑	<					>
B	<					>
-	<					>
\$			<	<	<	

o)

$$x \rightarrow x \oplus y/y$$

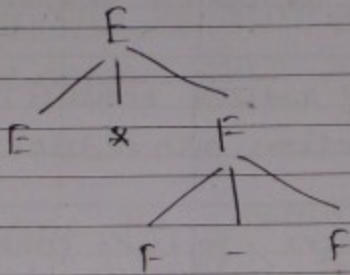
$$y \rightarrow z^* \quad y/z$$

$$z \rightarrow id$$



$$01 \quad E \rightarrow E * F / F + E / F$$

$$F \rightarrow F - F / id$$



"-" has highest precedence than + and *

III It will not work for partical compiler.

Drawback

I Not useful for (-x) operator
 unable to differentiate
 unary (-) and binary (-)
 (-3) (-4) assume no
 operators.

II power of this technique is very low.
 it suitable for very

$E \rightarrow E+E \mid E * E \mid id$

Note: LALR(1) parser tool, handle the -
ambiguous grammar by resolving the
conflict in the following manner,

In case of shift reduce conflict, priority is
given to shift action over reduce action.

In case of reduce - reduce conflict
priority is given for first reduce, production
over other reduce production.

Q) Consider the following grammar,
 $E \rightarrow E + E$ all is the above grammar
 $E \rightarrow E * E$ bed to, LALR(1) parser
 $E \rightarrow id$ tool, then which on of the
 following is true about the action
 take by the parser

1) it detect recursion and eliminate
 recursion

2) it detect, reduce - reduce conflict,
 and resolve the conflict by
 reducing the first production over
 other production.

3) if detect shift reduce conflict and resolve the conflict, in favour of -
reduce over, shift action

if detect shift reduce conflict and resolve the conflict in favour of -
shift action over reduce action.

Q2) assume the conflict are resolved in above manner, then what precedence and associativity rules parser realize and what is the value of the expression to be evaluate

$$3 * 2 + 1$$

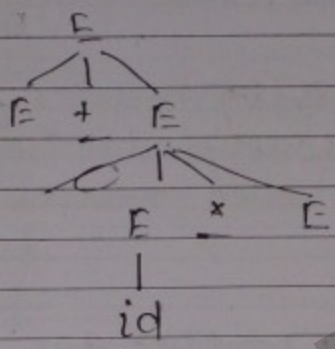
1) both + and * are same precedence and left associative expression value is '7'

2) both + and * are same precedence and expression value is '9' (right associative).

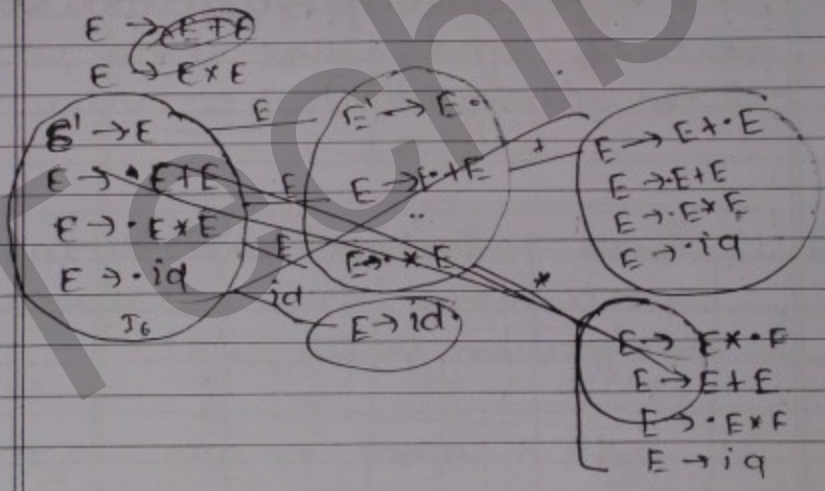
3) precedence of '*' is higher than '+' both are left associative value is '7'.

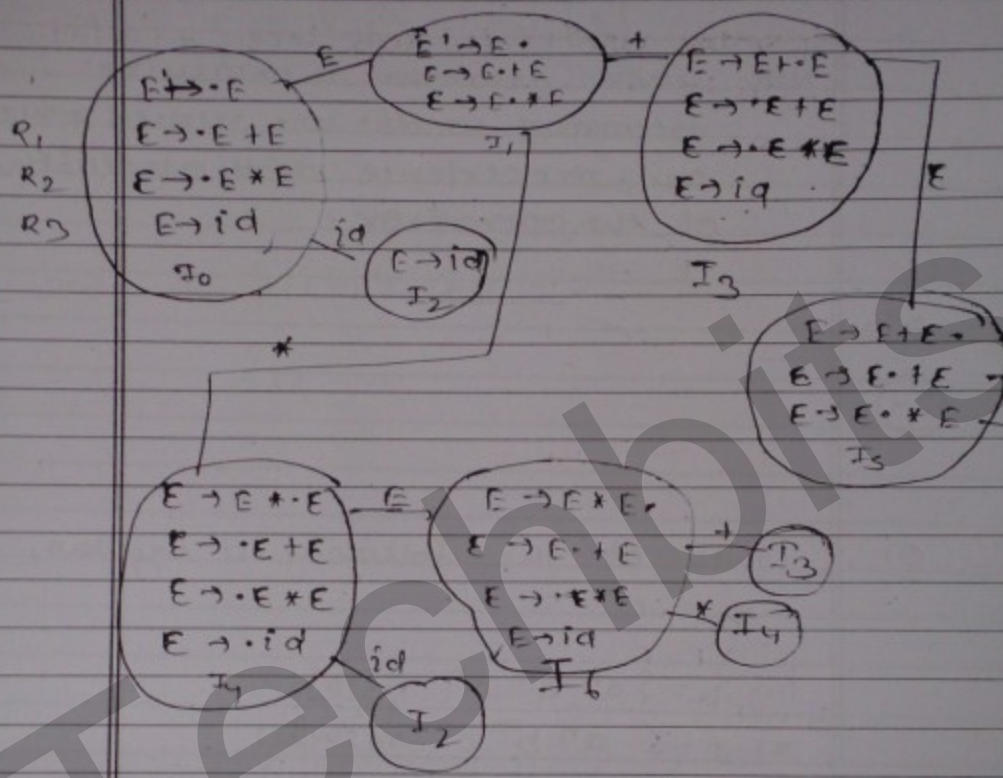
4) +, higher precedence than '*' and

operator are left associativ expression
valu is '9'.



71





	id	+	*	\$	E
I_0	S2				1
I_1		S3	S4	accept	
I_2		r3	r3	r3	
I_3	S2				5
I_4	S2				6
I_5	r1	r1	r1	r1	
I_6					

a, s, q

$$13) L = \{ w w^R \mid w \in \{a, b\}^* \}$$

$$14) L = \{ w x \}$$

$$20) L = \{ 1, 2, 4, 8, \dots, 2^n, \dots \}$$

all

#1 Every finite language are regular.

Any infinite language contain comparison
b/w symbol ~~is~~ non regular

In any language symbol power not
in "a.p" non regular.

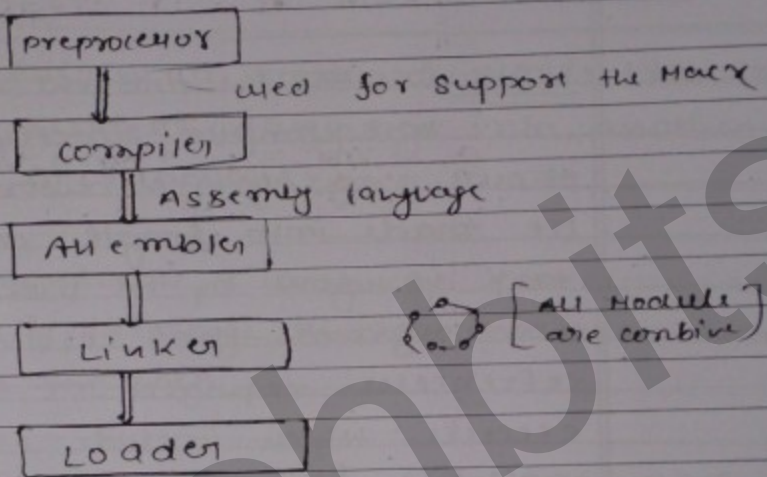

```
#include <stdio.h>
```

```
main()
```

```
{
```

```
printf("compiler");
```

```
}
```



preprocessor:- preprocessor take high level code as input, and it evaluate all the macro present in the program. which include `#include`, `#define` in C language and input statement in Java language

compiler:- compiler take preprocessor high level language and produce assembly language as output.

Assembler:- Assembler take assembly language as input and produce relocatable machine code (the machine code which can be moved in different place in memory).

Linker:- All the different modules of program are compile separately since to get output of our program. All different module can be made into single module the task is done by the linker. Hence linker is a program that resolve all external references required for the program to execute. which include machine code of predefined function (printf, scanf)

Loader:- Loader is a program that load executable machine code from secondary memory into main memory.

```

//
Main()
{
    printf("Hello");
}

```

Diff] compile

C. Compiler is a translator i.e. it translates one kind of language into another type of language.

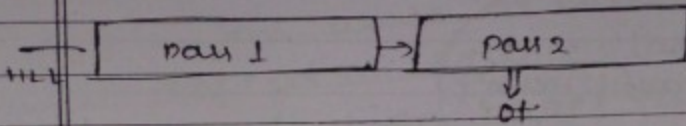
I. Interpreter is a language processor which take the language as input and execution done directly.

'C' whole program is translate at a time in compiler.

line by line execution will be done in interpreter.

compiler takes less time in compilation of program, compare to interpreter.

Where as interpreter take more time, in the interpretation of language bcoz line by line execution done.



ti pass :- one complete scan of the given -
High High table language called pass.

All Modern, compilers are multipass compilers because in multipass optimization of program perform.

ti phase :- The sub module of each pass is known as phase.

front end:- The phase of compiler which depend on source language and independent on target machine.

Backend:- The phase of compiler depend on target machine or independent on source.

Back = code optimization, code generation

Front = lexical, syntax, semantic, intermediate

Q.2)

7) b), 8) b), 9) b, 10) a) 12) b)

13) b, 14) b, 15) c, 16) b), 17) a)

$S \rightarrow aABe$
 $A \rightarrow Abc|b$
 $B \rightarrow d$

$aABe$

ϵ, a, A, aA, Ade $aABe$

$\epsilon, a, abcde$ $aAbcde$

$a(b)bcde$

viable

prefix

ϵ, a, ab

The prefix of handle left hand side in right sentential form are called as "viable prefix".

#

$S \rightarrow AB$

$S \rightarrow CA$

$B \rightarrow BC$

$B \rightarrow AB$

$A \rightarrow a$

NOTE

\Rightarrow In SLR(1), LALR shifted entries are same.

\Rightarrow no to part is same and

Reduced entries may be different

#

The following are the semantic error

- 1) using variable, without declaration
- 2) re-declaration of multiple variable
- 3) scope variable rule.
- 4) non compatible type expression
- 5) Mismatch of formal actual parameter.
- 6) Type mismatch in formal and actual parameter.

Context Sensitive grammars

↳ Attribute grammar will used.

C++ { Semantic rule }

used to handle the semantic change per

Syntax directed translation is formalization in which each grammar production is associated with, set of semantic rules.

f) functionality of (SDT)

1) It identifies all semantic errors and error messages to error handler.

2) It helps the construction of intermediate table.

3) Symbol table construction.

4) Construction of syntax ~~tree~~ tree.

Designing SDT

1) construct parse tree

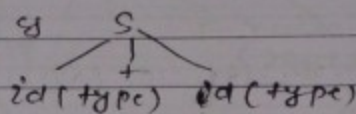
2) construct annotated parse tree

3) compute attribute values in annotated

parse ~~tree~~ ~~tree~~ tree.

5) generalize rules of attribute computation attached to grammar production which known as semantic rules.

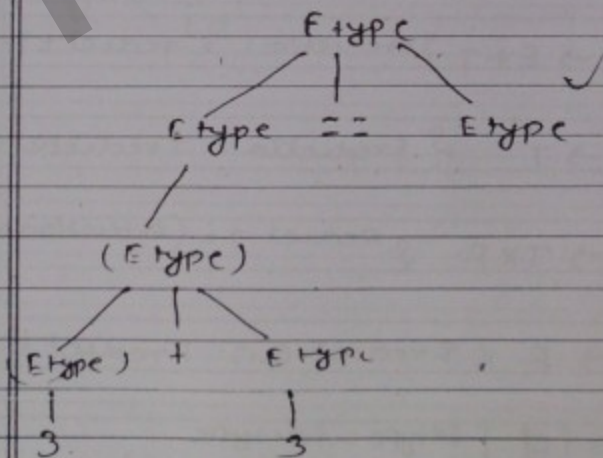
#1 Annotated parse tree: decorate parse tree.



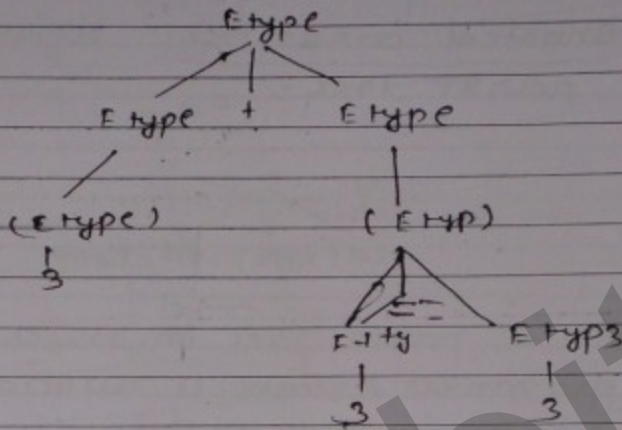
⇒ It is a parse tree in which each grammar symbol is associated with set of attribute values.

$E \rightarrow E + E$ [if ($E_1 \cdot \text{TYPE} = E_2 \cdot \text{TYPE}$) or ($E_1 \cdot \text{TYPE} = \text{int}$)
 $\wedge E \cdot \text{TYPE} = \text{int or float or int}$]
 $E \rightarrow (E)$ [$E \cdot \text{TYPE} = E_1 \cdot \text{TYPE}$]
 $E \rightarrow E == E$ [if ($E_1 \cdot \text{TYPE} = E_2 \cdot \text{TYPE}$) or ($E_1 \cdot \text{TYPE} = \text{int/boolean}$)
 $\wedge E \cdot \text{TYPE} = \text{boolean}$]
 $E \rightarrow \text{NUM}$ [$E \cdot \text{TYPE} = \text{non-type}$]
 $E \rightarrow \text{true}$ [$E \cdot \text{TYPE} = \text{boolean}$]
 $E \rightarrow \text{false}$ [$E \cdot \text{TYPE} = \text{boolean}$]

(3+3) == 6



01

 $3+(3==6)$ K

#

Construct the SDT that would give total no. of reduction take by bottom up parser, in construction of parse tree.

red is attribute and $E.red = \text{Total no. of reduction take by the parser}$. He construct SDT by follow grammar.

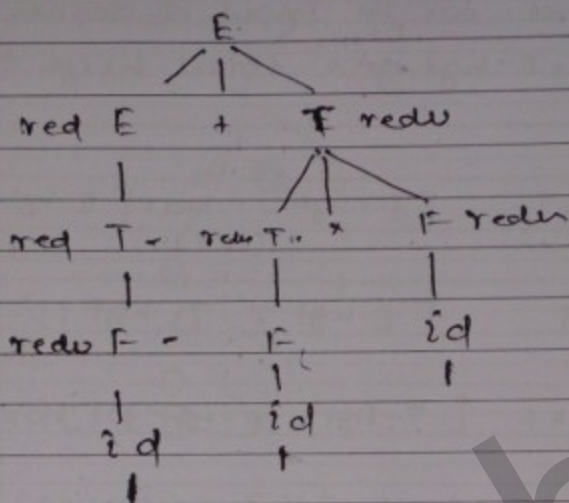
$$E \rightarrow E + T \quad \{ E.red = E.red + T.red + 1 \}$$

$$E \rightarrow T \quad \{ E.red = T.red + 1 \}$$

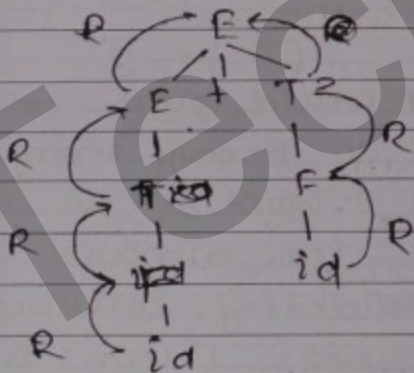
$$T \rightarrow T * F \quad \{ \text{Reduct } T = (\text{Reduction } T + \text{Reduction } F) + 1 \}$$

$$T \rightarrow F \quad \{ T.red = F.red + 1 \}$$

$$F \rightarrow id \quad \left[\begin{array}{l} E.type = id.type \\ F.red = 1 \end{array} \right]$$



†1 Reduct to a+b



#1 Construct a BD that would calculate height of parse tree. for the input is derived. where
 $B \cdot \text{Hgt}$, $F \cdot \text{hgt}$ give total height of parse tree

$$E \rightarrow E + T \quad [E \cdot \text{hgt} = \max[E \cdot \text{hgt}, T \cdot \text{hgt}] + 1]$$

$$E \rightarrow T \quad [E \cdot \text{hgt} = T \cdot \text{hgt} + 1]$$

$$T \rightarrow T * F \quad [T \cdot \text{hgt} = \max[T \cdot \text{hgt}, F \cdot \text{hgt}] + 1]$$

$$T \rightarrow F \quad [T \cdot \text{hgt} = F \cdot \text{hgt} + 1]$$

$$F \rightarrow \text{id} \quad [F \cdot \text{hgt} = 1]$$

Q1 Construct that would count, total no. of 1's present in binary string. where count is attribute. S. count give the total no. of

PS: count: S → α α's in binary string by considering following grammar.

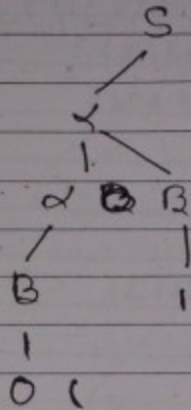
$$\alpha \rightarrow \alpha B \quad [L \cdot \text{count} = L \cdot \text{count} + B \cdot \text{count}]$$

$$\alpha \rightarrow B \quad [L \cdot \text{count} = B \cdot \text{count} + 1]$$

$$B \rightarrow 1 \quad [B \cdot \text{count} = 1]$$

$$B \rightarrow 0 \quad [B \cdot \text{count} = 0]$$

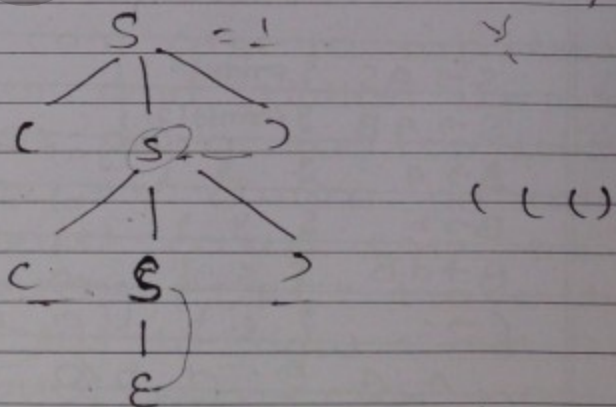
11001



Q1 Construct SDT that would give total no of balanced parentheses present in input string

$S \rightarrow (S) \quad S\text{-count} = S\text{-count} + 1$

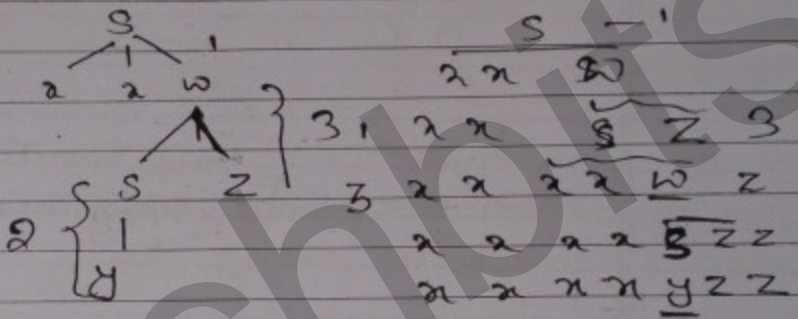
$S \rightarrow \epsilon \quad S\text{-count} = 0$



 $S \rightarrow xwx \ \& \ \text{printf}(1)$
 $S \rightarrow Y \ \& \ \text{printf}(2)$
 $w \rightarrow SZ \ \& \ \text{printf}(3)$

$xxxxyz$

a) 12313 b) 23131 c) 13112 d) None



2
 2 3 1 3 1

a) $S \rightarrow AS \ \& \ \text{printf}(1)$

$S \rightarrow AB \ \& \ \text{printf}(2)$

$A \rightarrow a \ \& \ 3$

$B \rightarrow b \ \& \ 4$

$B \rightarrow dB \ \& \ 5$

$C \rightarrow c \ \& \ c$

a) 666453211

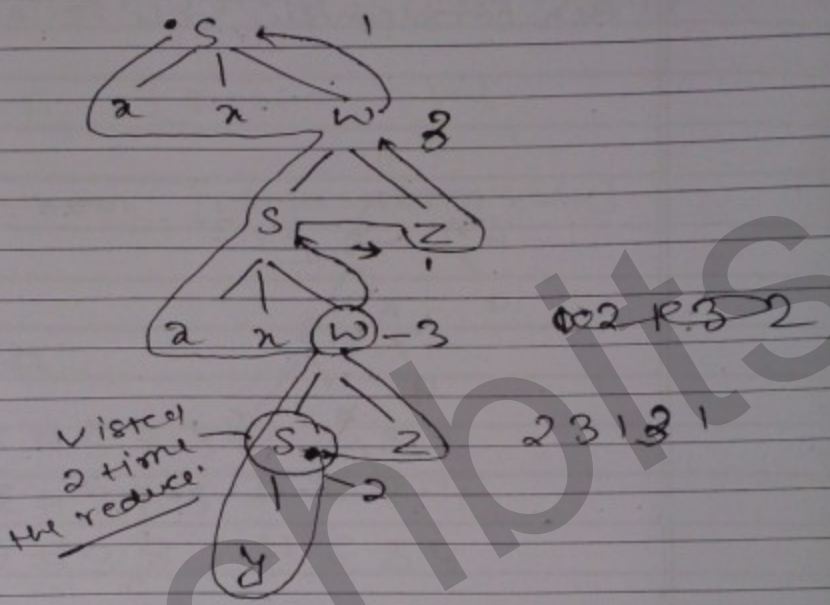
b) 33364521

c) 333641251

d) None

~~$A \ A \ A \ d \ b \ c \ a \ a \ a \ d \ b \ c$~~
 $A \ A \ a \ d \ b \ c = 3$
 $A \ a \ a \ d \ b \ c = 3$
 $a \ a \ a \ d \ b \ c$

Top down parser (LRT most)



parse tree creat:

NOTE

SDT can give to top down parser and bottom up parser. If SDT given to top down parser, top down parser construct parse tree by traversing "DFS" traversal from left to right. In DFS traversal when ever node is visited two time correspondingly rule is executed.

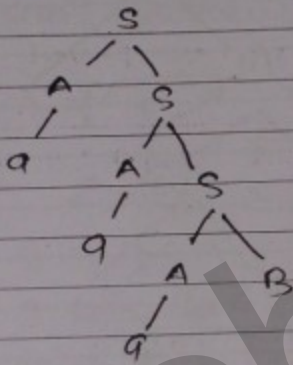
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if SDT is given to bottom up parser,
when ever reduced action it ~~is~~ popping
then correspondly rule is executed.



$$Q) \quad E \rightarrow E, \#T \quad \{E.val = E_1.red \neq T.val\}$$

$$E \rightarrow T \quad \{E.val = T.val\}$$

$$T \rightarrow T_1 \& F \quad \{F.val = T_1.val * F.val\}$$

$$2 \quad T \rightarrow F \quad [T.val = F.val]$$

$$2 \quad F \rightarrow \text{num} \quad [F.val = \text{num.value}]$$

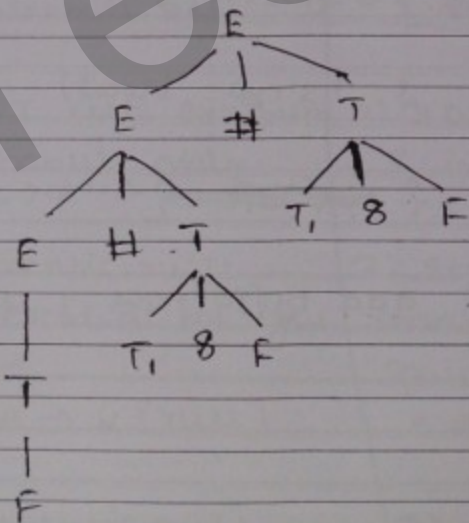
~~2 #~~

T # 3 8 5 # 6 8 4

~~T~~ # 3 8 5 # 6 8 4

2 # 3 8 5 # 6 8 4

2



Synthesized attribute :- The attribute value at a node is computed in terms of its children in the annotated parse tree such type of attribute known as synthesized attribute
(well suitable for = bottom up)

Inherited attribute :- The attribute value at a node in the annotated parse tree, is computed either from parents, or from the left sibling. It known as, inherited attribute.
(suitable = top down)

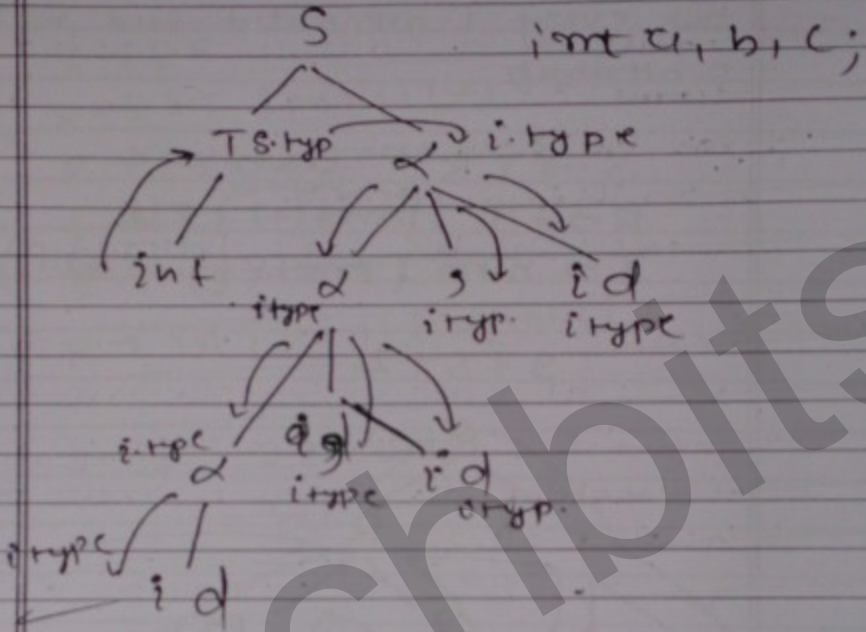
$S \rightarrow T \ \& \ S \ \& \ \{ \text{type} = T.\text{stype} \}$

$T \rightarrow \text{int} \ \& \ \{ \text{stype} = \text{int} \}$

$T \rightarrow \text{float} \ \& \ \{ \text{stype} = \text{float} \}$

$\alpha \Rightarrow \alpha.\text{id} \ \& \ \{ \text{stype} = \alpha.\text{stype} \}$

$\alpha \Rightarrow \text{id} \ \& \ \text{add ty}(\text{id}, \text{name}, L.\text{stype})$

SDTS.

Q1

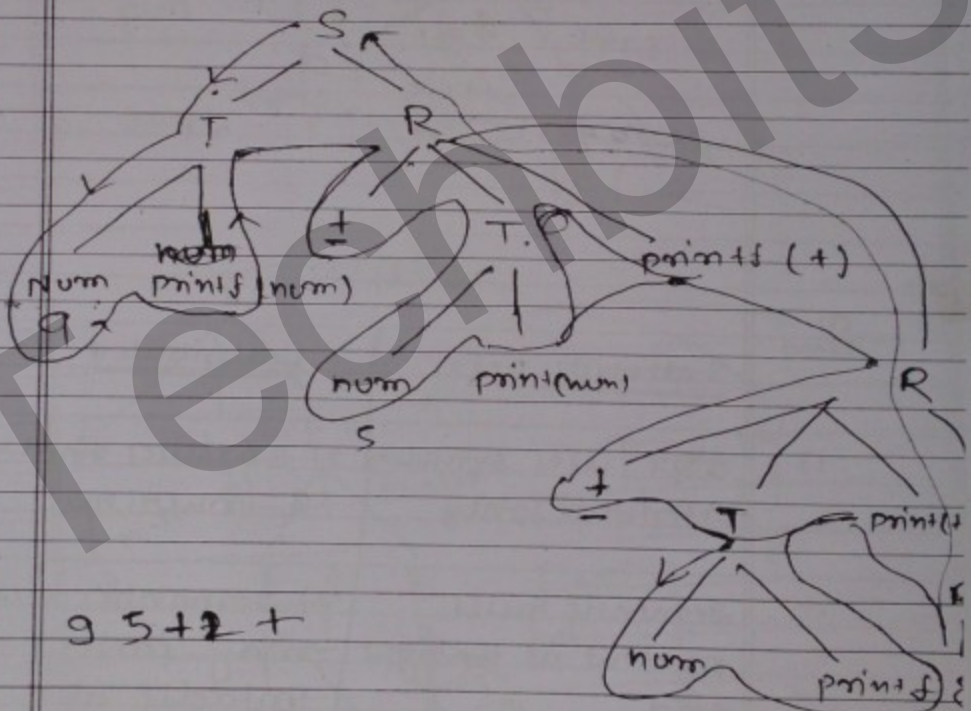
S-attribute DefL-attribute

- | | |
|---|--|
| 1) SDT w/c syntactic attribute only | 2) SDT w/c synthesized & inherited. |
| 2) Semantic rule present at the right end
$A \rightarrow \alpha [\text{rule}]$ | 2) Semantic rule may present in the middle also.
$A \Rightarrow \alpha \{ \text{rule} \} \beta$ |
| 3) Semantic rule evaluates in bottom-up parser | 3) Rule are evaluated in DFS. |

Q1) Every S' attributed def is L- attributed def
 but every L- attributed need not to be S attribute.

$S \rightarrow TR$ L- attributed d.
 $R \rightarrow +T \{ \text{print}(+) \} R | \epsilon$
 $T \rightarrow \text{num} \{ \text{print}(f(\text{num value})) \}$

9 + 5 + 2



9 5 + 2 +

Consider the following SMT

$$S \rightarrow ER$$

$$R \rightarrow *E \{ \text{print} + S(*) \} R / E$$

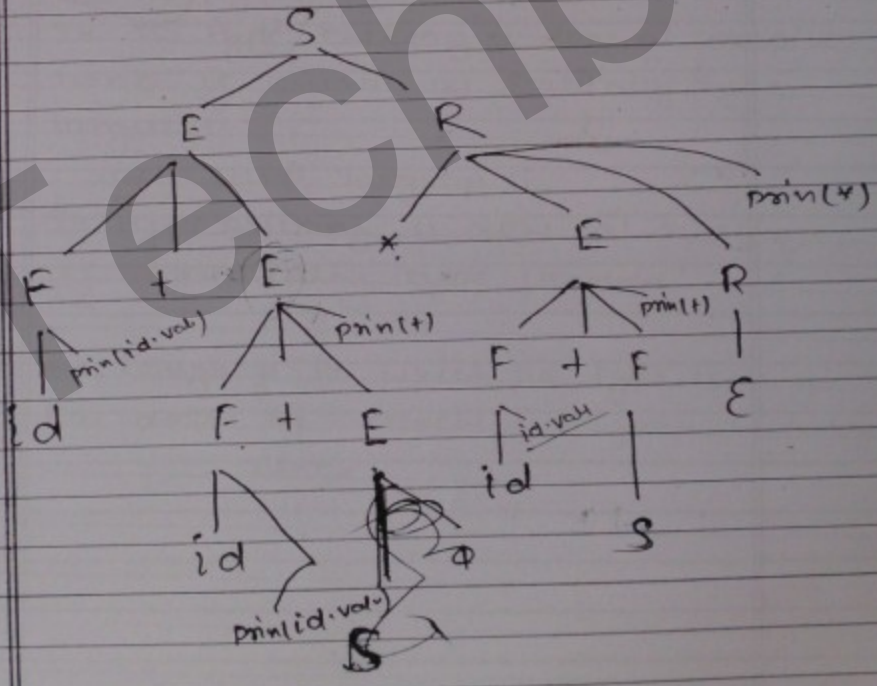
$$E \rightarrow F + E \{ \text{print} + (+) \}$$

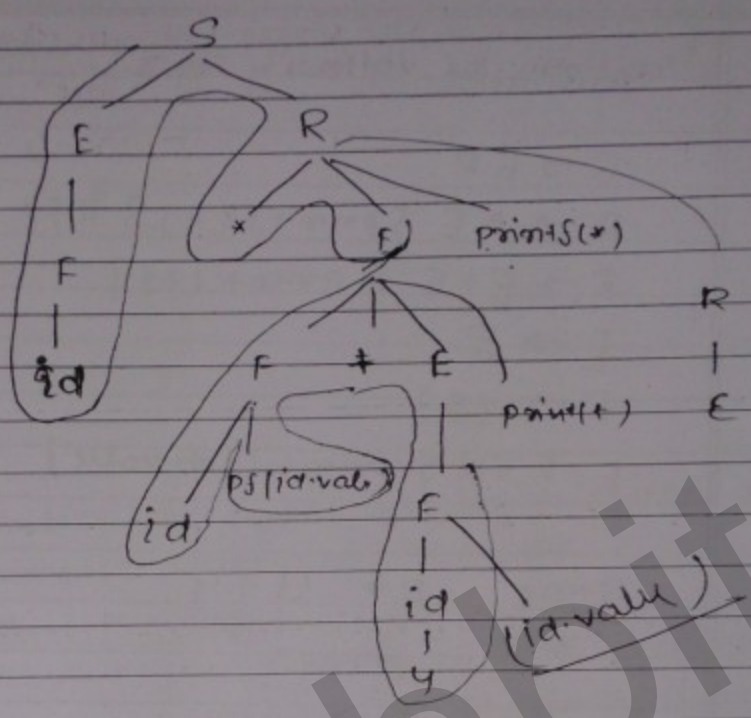
$$E \rightarrow F$$

$$E \rightarrow (S)$$

$$F \rightarrow id \{ \text{print} + (id \cdot \text{val}) \}$$

String $2 * 3 + 4$





Techbits

- #1 Construct the S.T.D. that perform type conversion by consider type conversion done in integer and real value.

$$E \rightarrow E+T \dots$$

$$E \rightarrow T$$

- #1 Statically type checking will done at compile time and runtime.

eg C language

- #1 If the type checking is done at compile time it known as statically type language:

eg LISP language.

- #1 If type checking is done at runtime, it dynamically type language:

- #1 the language in which no type checking will done: eg = Machine language, Assembly language